

DEEP LEARNING

Lecture 14: Meta-Learning

Dr. Yang Lu

Department of Computer Science and Technology

luyang@xmu.edu.cn



What is Meta?

- When meta is used as a single word, it refers to itself or to the conventions of its genre, self-referential.
- The chinese translation is 元.



What is Meta?

- When meta is used as a prefix, meta-X means “beyond-X,” “after-X,” or “X about X”.
- Examples:
 - Metadata: data that describes other data.
 - Metafile: in computer graphics, define objects and images using a list of coordinates.
 - Metaphysics (形而上学): a branch of philosophy that examines the fundamental nature of reality.
 - Meta-analysis: a statistical analysis that combines the results of multiple scientific studies.
 - Metaverse: a virtual world supporting persistent online 3-D virtual environments.

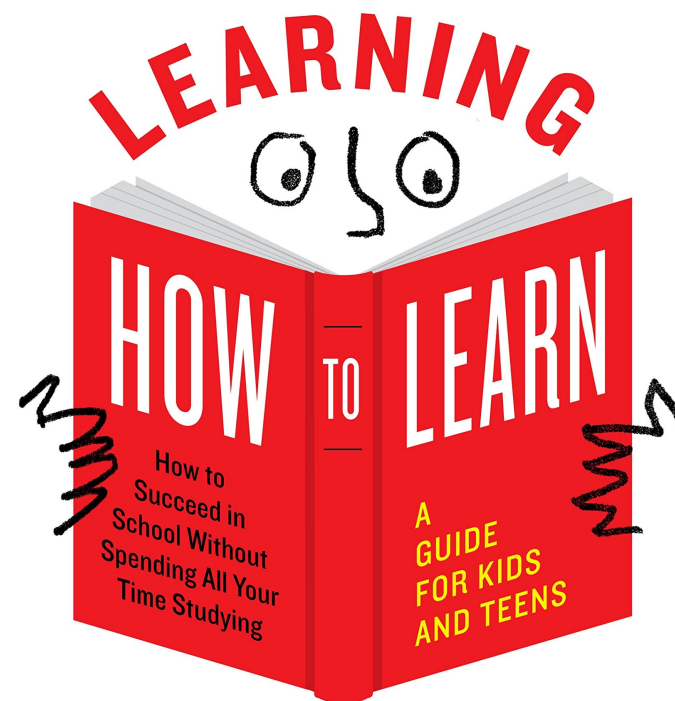


Meta-Learning

- Meta-learning (元学习) also means “beyond learning”, “above learning” or “learning about learning”.
- It has another name:

Learning to learn

From the bestselling author of *A Mind for Numbers* and the creators of the popular online course Learning How to Learn



BARBARA OAKLEY, PhD, AND
TERRENCE SEJNOWSKI, PhD,
WITH ALISTAIR McCONVILLE



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Image source: <https://images-na.ssl-images-amazon.com/images/I/81j+JH7WshL.jpg>

Meta-Learning

- Historically, the success of **machine learning** was driven by the choice of hand-engineered features with **model learning**.
 - Problem: how to select feature...
- **Deep learning** realized the promise of **joint feature and model learning**, providing a huge improvement in performance for many tasks.
 - Problem: how to select algorithm/hyperparameter...
- **Meta-learning** in neural networks can be seen as aiming to provide the next step of integrating **joint feature, model, and algorithm learning**.



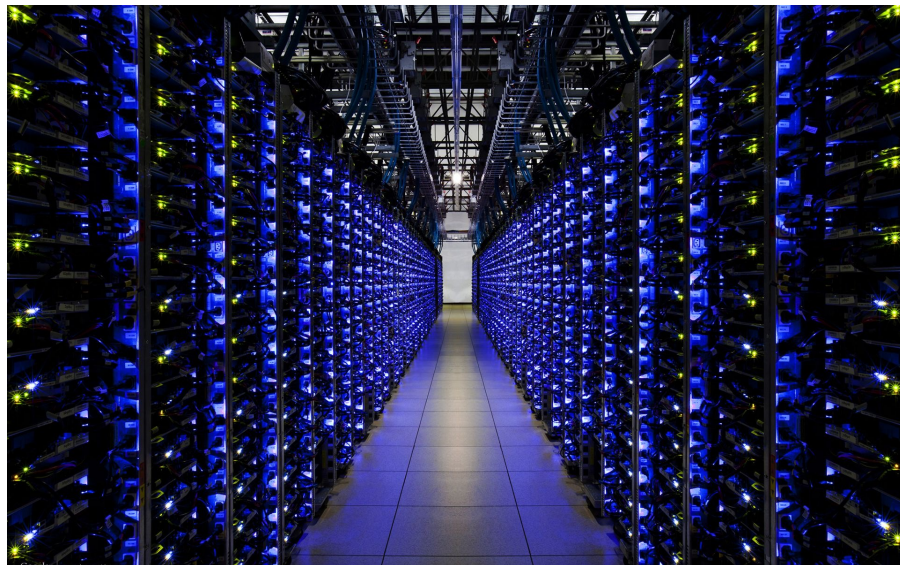
Algorithm Learning

- Learning aspects:
 - Model learning: select the best model for the task.
 - Feature learning: select the best feature for the task.
 - Algorithm learning: select the best algorithm for the task.
- How do we select an algorithm to train a model?
 - Manually try different algorithms.
 - Manually try an algorithm with different hyperparameters.



Algorithm Selection vs. Algorithm Learning

Industry



Using 1000 GPUs to try 1000
sets of hyperparameters

Academia



Randomly choose a set by imagination
and claim that it is the best!

Meta-learning automates this procedure by end-to-end neural networks.



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Image source: https://www.xinxiang.com.cn/xinxiang/2015/01/16/1501160526_HIST_%E7%85%89%E4%B8%B9_%E7%A7%A6%E5%A7%8B%E7%9A%87F.jpg

https://media.bastillepost.com/wp-content/uploads/hongkong/2016/05/20160526_HIST_%E7%85%89%E4%B8%B9_%E7%A7%A6%E5%A7%8B%E7%9A%87F.jpg



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Relation to AutoML

- AutoML aims to automate parts of the machine learning process that are typically manual.
 - Such as data preparation, algorithm selection, hyperparameter tuning, and architecture search.
- AutoML sometimes makes use of end-to-end optimization.
 - Meta-learning can be seen as a specialization of AutoML.
- Meta-learning is about algorithm learning, rather than algorithm tuning.



Google Cloud
AutoML



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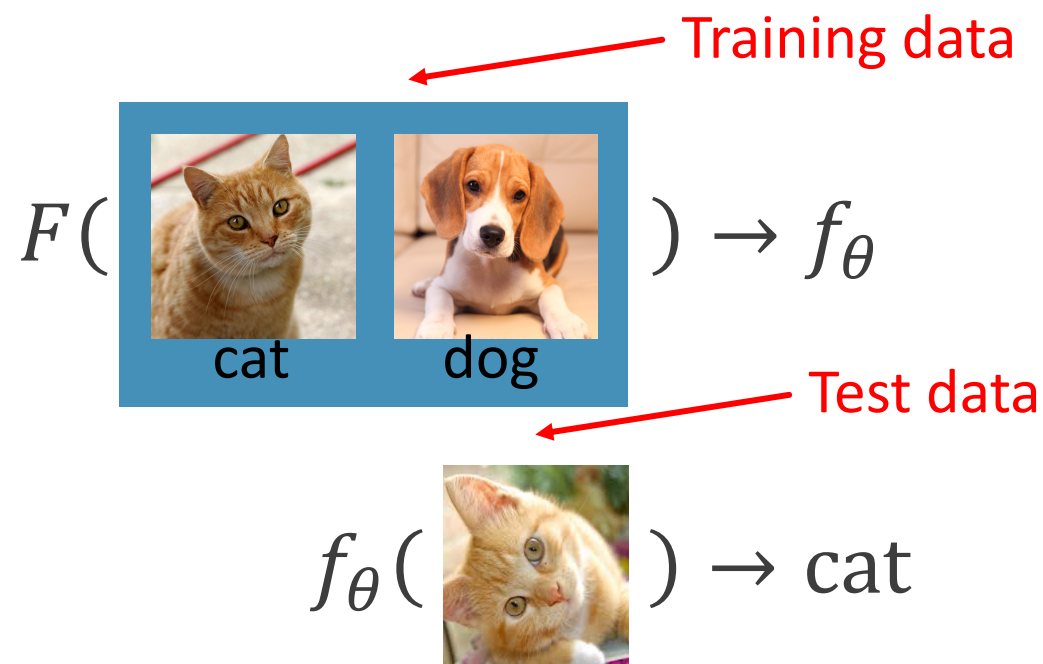
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Image source: <https://www.datanami.com/2018/01/17/google-automate-machine-learning-automl-service/>

From Machine Learning to Meta-Learning

- In machine learning, we select an algorithm F , train it by optimizing the parameter θ , and obtain model f_θ .

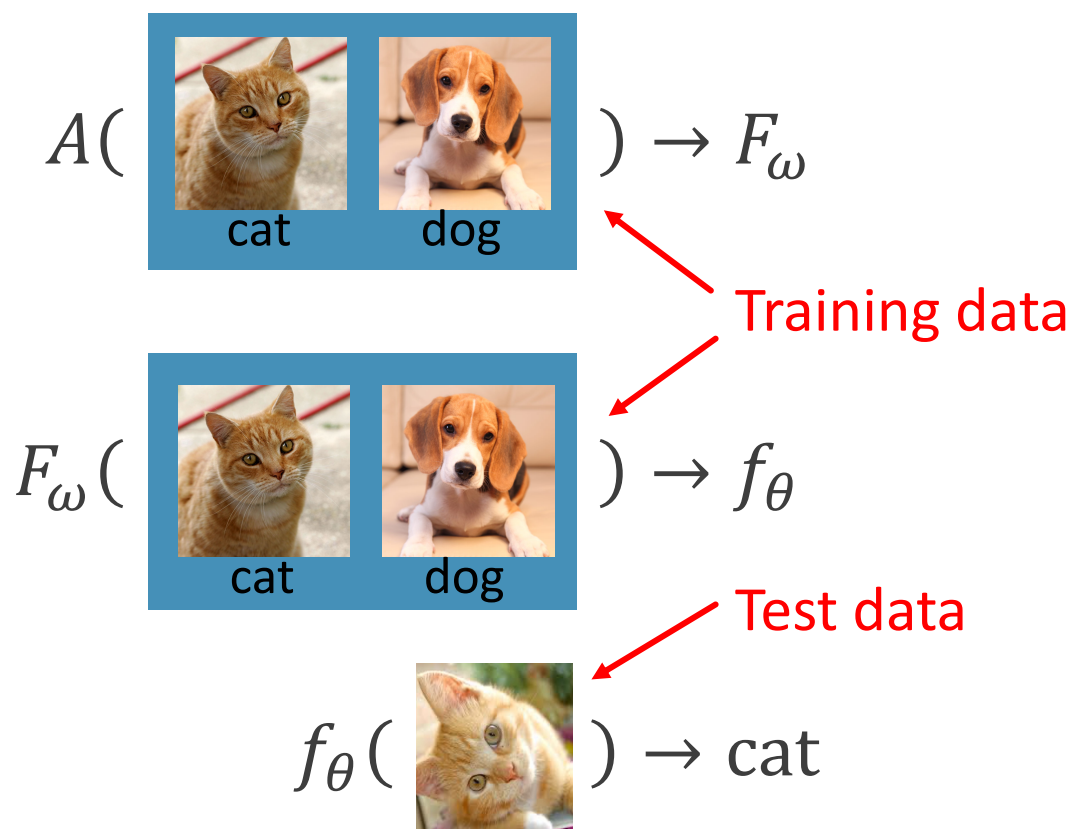


By the idea of learning to learn, can we learn F ?



From Machine Learning to Meta-Learning

- Now, our goal is to find the best algorithm F for the task, just like the best model f for the data.

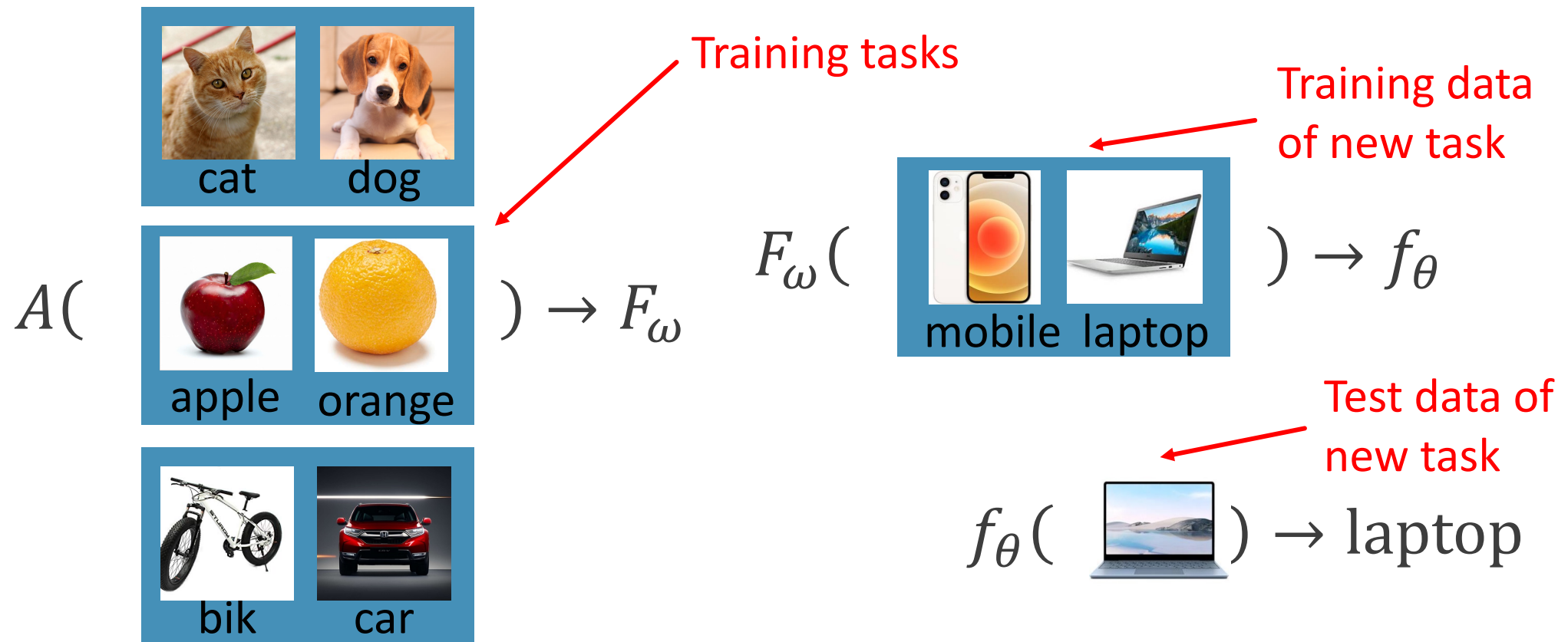


ω is learnable algorithm parameters. It is usually called meta-knowledge.



From Machine Learning to Meta-Learning

- When we deal with multiple tasks, we can also train F_ω to be good for all tasks. In this way, it is capable of generalizing new task.



Single-Task and Multi-Task Meta-Learning

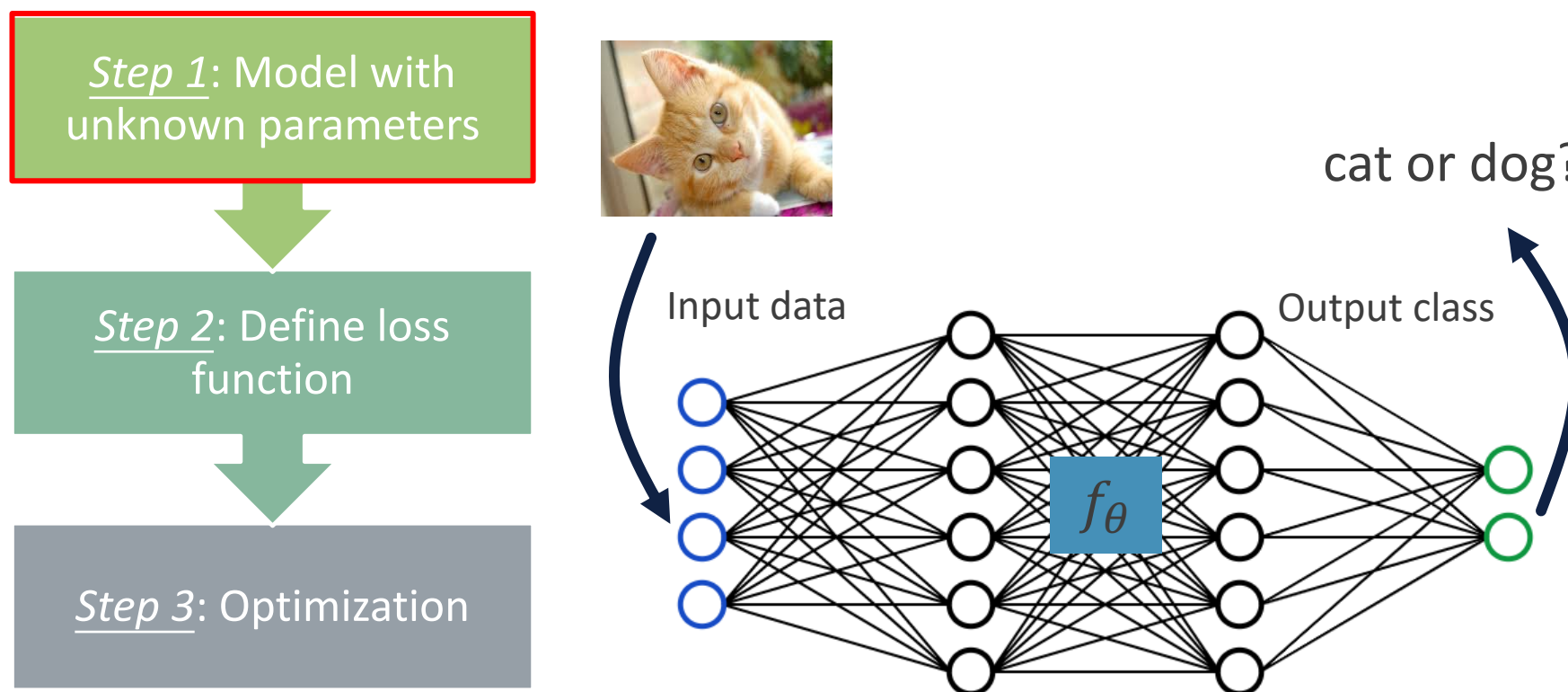
- Single-task and multi-task meta-learning actually deals with different problems.
- Single-task meta-learning aims at learning the most suitable algorithm for this task.
- Multi-task meta-learning aims at learning the most suitable algorithm for all tasks, **and be capable of dealing with new task.**

Notice the difference between multi-task meta-learning and multi-task learning.

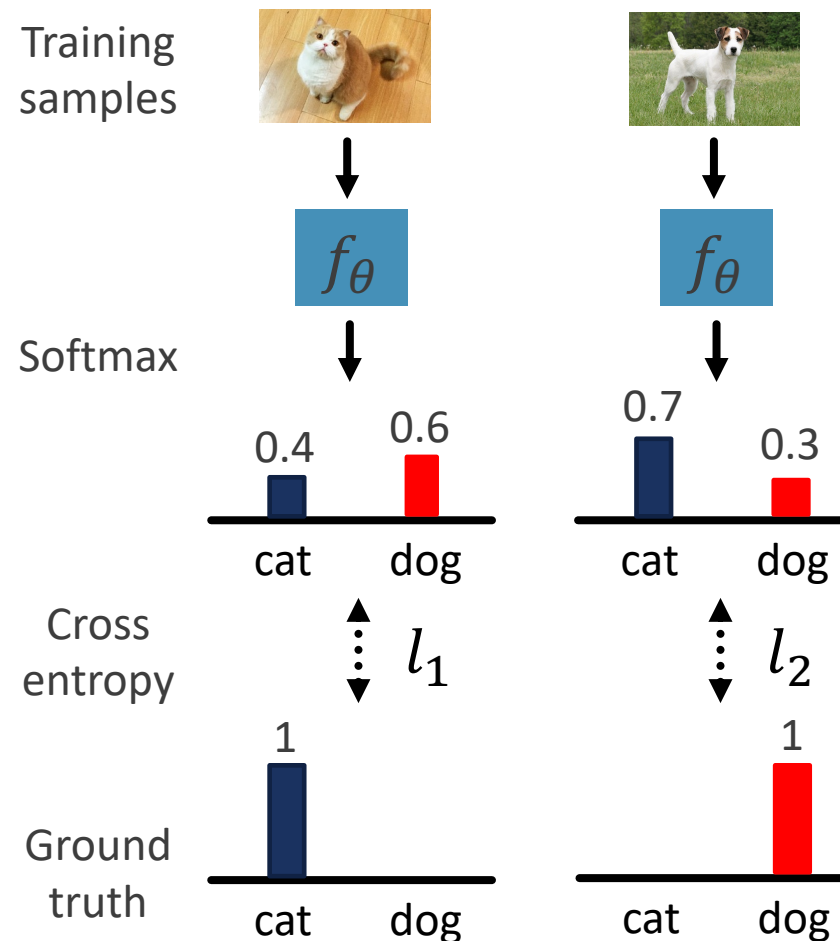
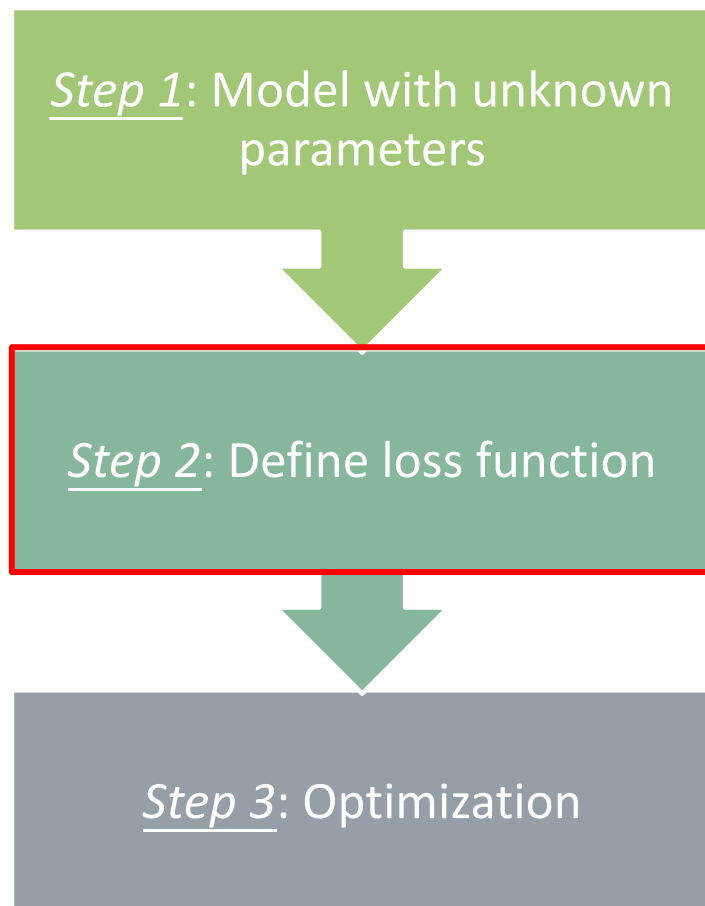


How to Learn Model Parameter?

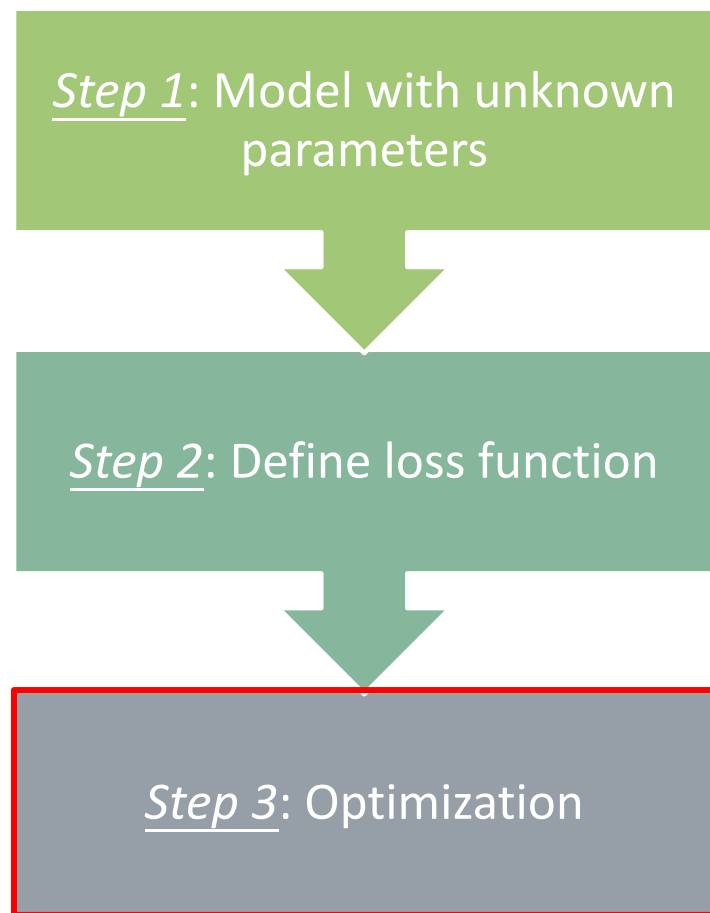
- Now, the problem is **how to learn algorithm parameter ω** ?
- Recall that how we learn model parameter θ .



How to Learn Model Parameter?



How to Learn Model Parameter?



loss: $L(\theta) = \sum_{i=1}^{|D|} l_i$ sum over training examples

$$\theta^* = \underset{\theta}{\operatorname{argmin}} L(\theta)$$

done by gradient descent

f_{θ^*} is the model learned by a learning algorithm from data.

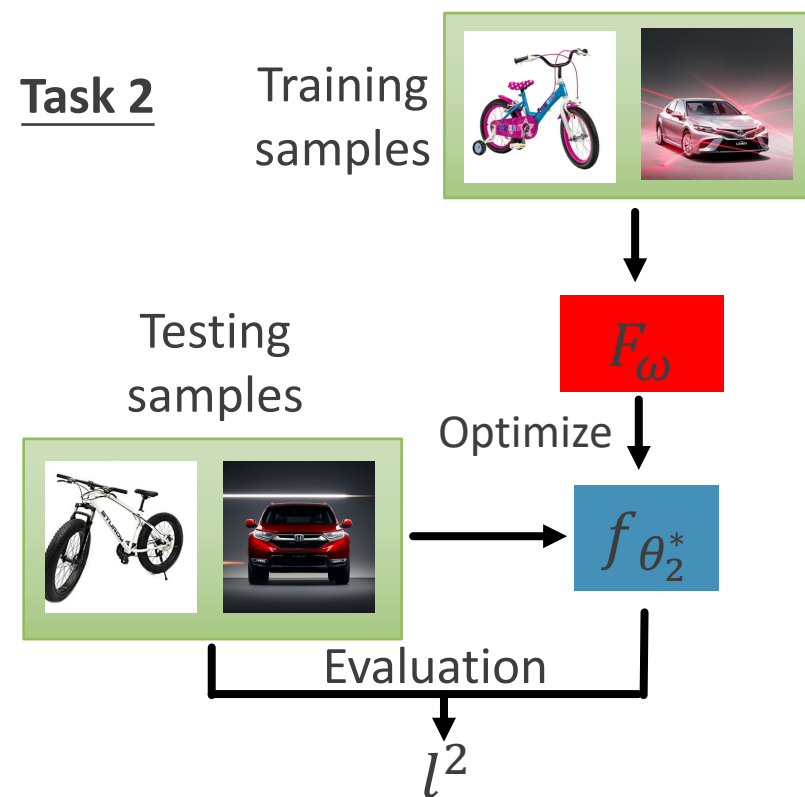
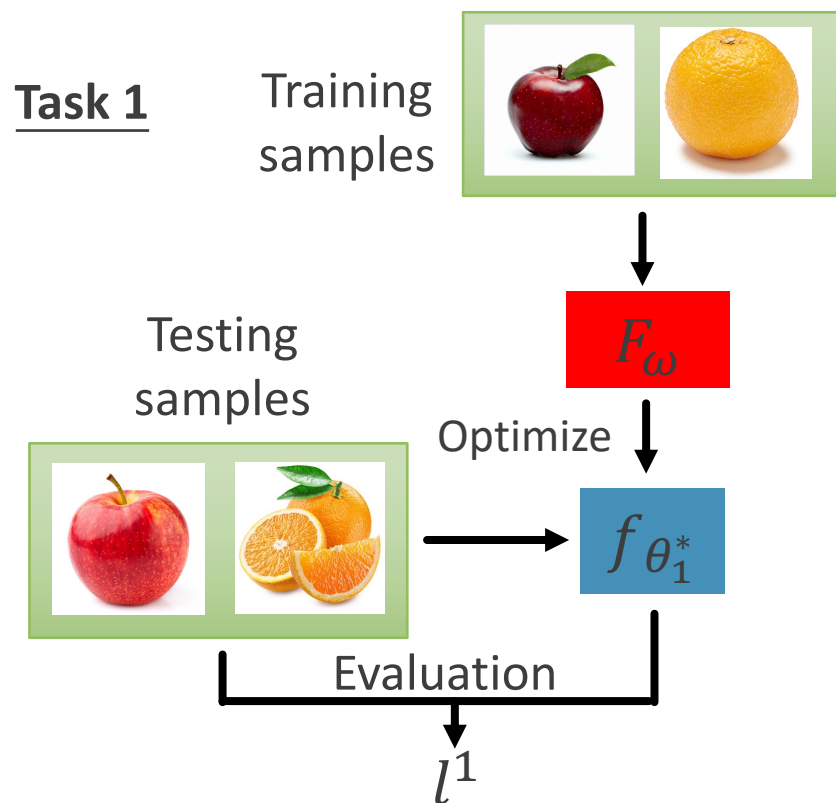


How to Learn Algorithm Parameter?

- Learning algorithm parameter is exactly same as learning model parameter.
- Instead of generalizing over data, it generalizes over tasks.



How to Learn Algorithm Parameter?



$$\text{Total loss: } L(\phi) = \sum_{n=1}^N l^n$$

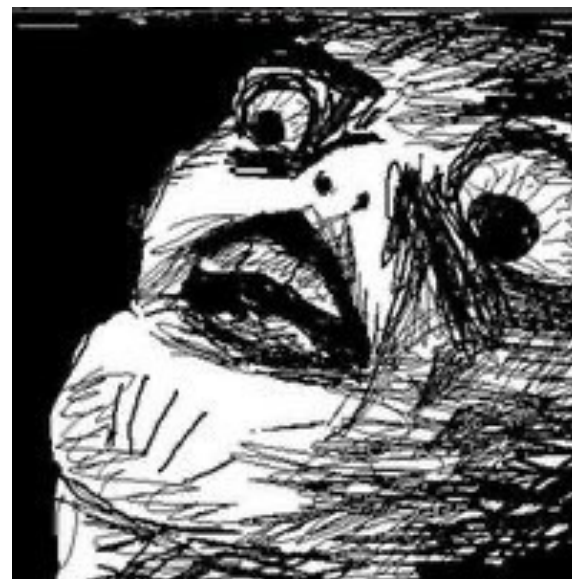
(N is the number of the training tasks)



How to Learn Algorithm Parameter?

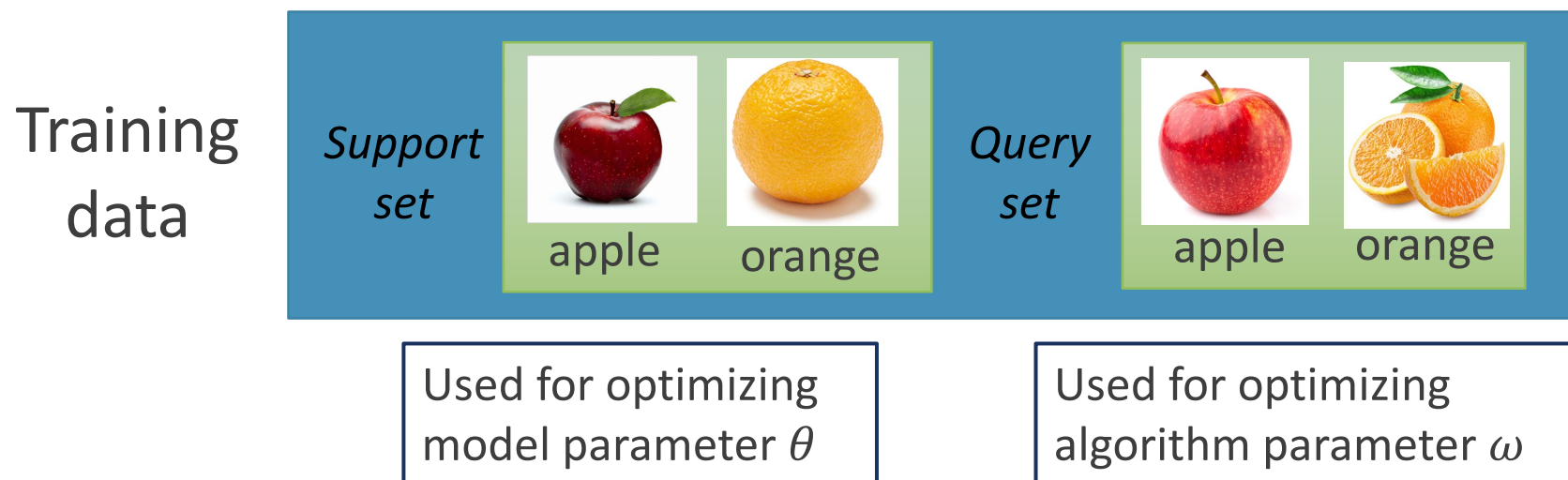
- In typical machine learning, the loss is computed based on training examples.
- In meta-learning, the loss is computed based on testing examples.
- Is there any problem here?

You dare use testing data during training!



How to Learn Algorithm Parameter?

- However, we have to use “testing data” to evaluate how the algorithm parameter performs.
- We can cut a part from the training data, just like validation data.

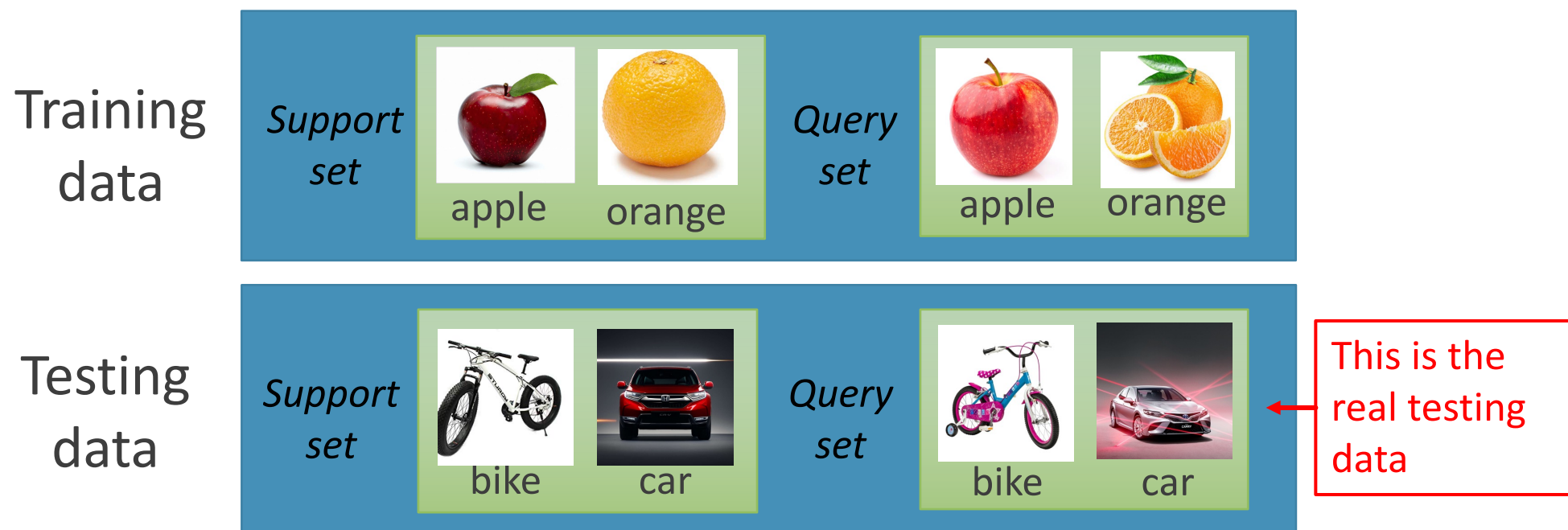


Query set is nothing but “validation data for training”



How to Learn Algorithm Parameter?

- Similarly, we also split testing data into support and query set.
- The label of testing support set is available during testing.
- The testing query set is the real testing data to evaluate the performance of meta-learning algorithm.



Formalizing Meta-Learning

- Training and testing phases in meta-learning is called meta-training and meta-testing.

- Meta-training can be formalized as bi-level optimization:

Outer loop

$$\omega^* = \operatorname{argmin}_{\omega} \sum_{i=1}^M L^{meta} \left(\theta^{*(i)}(\omega), D_{train}^{query(i)} \right)$$

Loss to evaluate algorithm

Inner loop

$$s.t. \theta^{*(i)}(\omega) = \operatorname{argmin}_{\theta} L^{task} \left(\theta, \omega, D_{train}^{support(i)} \right)$$

Loss to evaluate model

- Meta-testing for new task j can be formalized as:

$$\theta^* = \operatorname{argmin}_{\theta} L^{task} \left(\theta, \omega^*, D_{test}^{support(j)} \right)$$

And finally we use f_{θ^*} to predict samples in $D_{test}^{query(j)}$.



Few-Shot Learning

- One direct application of multi-task meta-learning is **few-shot learning (小样本学习)**.
- Do we human beings need great amount of training data to recognize image category?
- **No! We have the learning ability. We know how to learn!**
 - When we deal with new task, our experience help us learn with only a few samples.
 - We are experts of “learning to learn”.



- Have you seen before an okapi?
- Can you learn to recognize it from only this image?



Few-Shot Learning

Training task 1

Support set

$K=2$



$N=3$

Query set



Training task 2 . . .

Support set



Query set

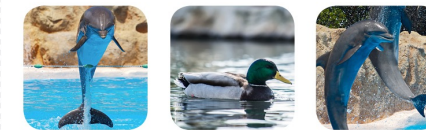


Test task 1 . . .

Support set



Query set



A typical setting for few-shot learning: *n*-way-*k*-shot
k is usually set at 1 or 5



Setting of Few-Shot Learning

- Few-shot learning has its own benchmark datasets.
 - MinilmaNet, Fewshot-CIFAR100, Omniglot, etc.
- A typical dataset split for MinilmaNet is: 64 training classes, 12 validation classes, and 24 test classes.
 - No class overlap among training, validating and test.
- We run a lot of episodes for training. In each episode, we randomly select N classes with $k + 1$ samples.
 - k support samples and 1 query sample.



Few-Shot Classification Leaderboard

*mini*ImageNet Leaderboard (5-class)

[Edit this leaderboard](#)

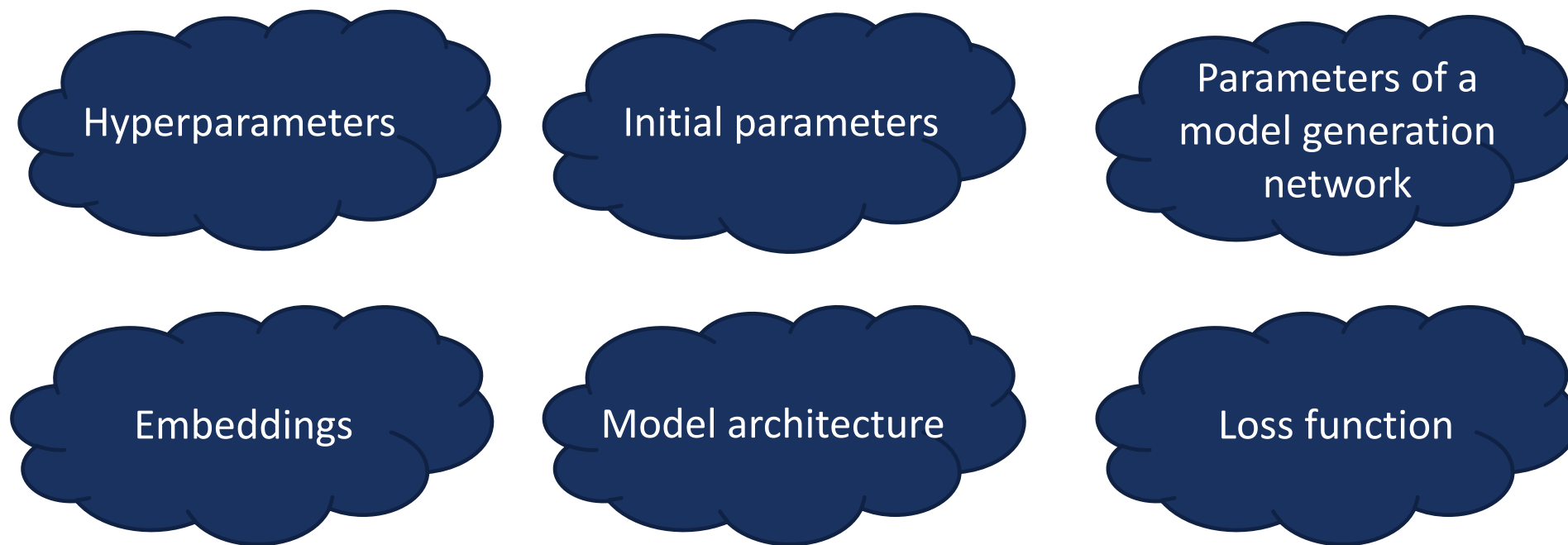
Search:

| Method | Venue | Year | Backbone | Setting | 1-shot | 5-shot | Code | Reported by |
|----------------------------------|-------|------|------------------------------------|-----------------|------------------|------------------|---------------------------|--------------------------|
| EASY | arXiv | 2022 | 3xResNet012 | Transductive | 84.04 \pm 0.23 | 89.14 \pm 0.11 | [PyTorch] | [Source] |
| iLPC | ICCV | 2021 | WRN-28-10 | Semi-supervised | 83.58 \pm 0.79 | 89.68 \pm 0.37 | [PyTorch] | [Source] |
| iLPC | ICCV | 2021 | WRN-28-10 | Transductive | 83.05 \pm 0.79 | 88.82 \pm 0.42 | [PyTorch] | [Source] |
| PT+MAP | arXiv | 2021 | WRN | Transductive | 82.92 \pm 0.26 | 88.82 \pm 0.13 | [PyTorch] | [Source] |
| PTN | AAAI | 2021 | WRN-28-10 | Semi-supervised | 82.66 \pm 0.97 | 88.43 \pm 0.67 | None | [Source] |
| EASY | arXiv | 2022 | 2xResNet-12(1/ $\sqrt{2}$) | Transductive | 82.31 \pm 0.24 | 88.57 \pm 0.12 | [PyTorch] | [Source] |
| Simple CNAPS | CVPR | 2020 | ResNet18 (pre-trained on ImageNet) | Inductive | 82.16 | 89.80 | [PyTorch] | [Source] |
| Oblique Manifold | ICCV | 2021 | WRN-28-10 | Transductive | 80.64 \pm 0.34 | 89.39 \pm 0.39 | [PyTorch] | [Source] |
| ICA + MSP | ECCV | 2020 | DenseNet | Semi-supervised | 80.11 \pm 0.25 | 85.78 \pm 0.13 | None | [Source] |
| EPNet | ECCV | 2020 | WRN-28-10 | Semi-supervised | 79.22 \pm 0.92 | 88.05 \pm 0.51 | [PyTorch] | [Source] |



Meta-Knowledge

- Talking so much about the learnable algorithm F_{ω} .
- What exactly are those algorithm parameters ω ?



Meta-Knowledge Taxonomy

- Optimization-based Method
- Model-based Method
- Metric-based Method





OPTIMIZATION-BASED METHOD



Optimization-Based Method

- The meta-knowledge ω is related to the optimization process.
 - Learning to optimize
 - Learning to initialize
 - Learning to weight
 - Learning to reward
 - Learning to augment
 - Dataset distillation
 - Neural architecture search



Learning to learn by gradient descent by gradient descent

**Marcin Andrychowicz¹, Misha Denil¹, Sergio Gómez Colmenarejo¹, Matthew W. Hoffman¹,
David Pfau¹, Tom Schaul¹, Brendan Shillingford^{1,2}, Nando de Freitas^{1,2,3}**

¹Google DeepMind ²University of Oxford ³Canadian Institute for Advanced Research

`marcin.andrychowicz@gmail.com`

`{mdenil,sergomez,mwhoffman,pfau,schaul}@google.com`

`brendan.shillingford@cs.ox.ac.uk, nandodef Freitas@google.com`



Learning to Optimize

- Conventionally, when we do optimization

$$\theta_{t+1} \leftarrow \theta_t + \lambda g(\nabla_{\theta} L(\theta_t))$$

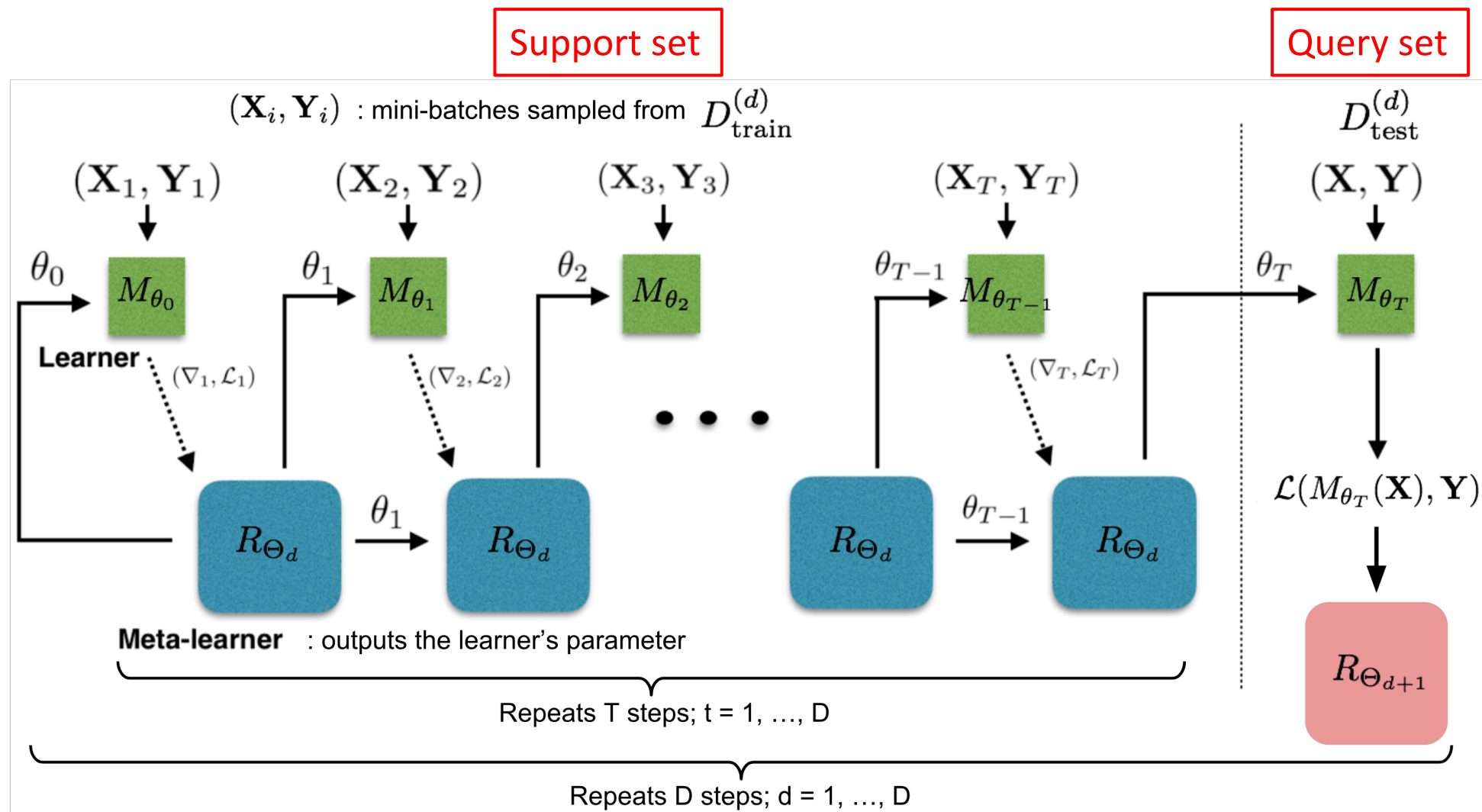
we select the optimizer g such as SGD, momentum, AdaGrad, ADAM, etc.

- g can be seen as a hand-crafted function of the gradients.
- In meta-learning, we can learn proper optimization function by meta-knowledge ω :

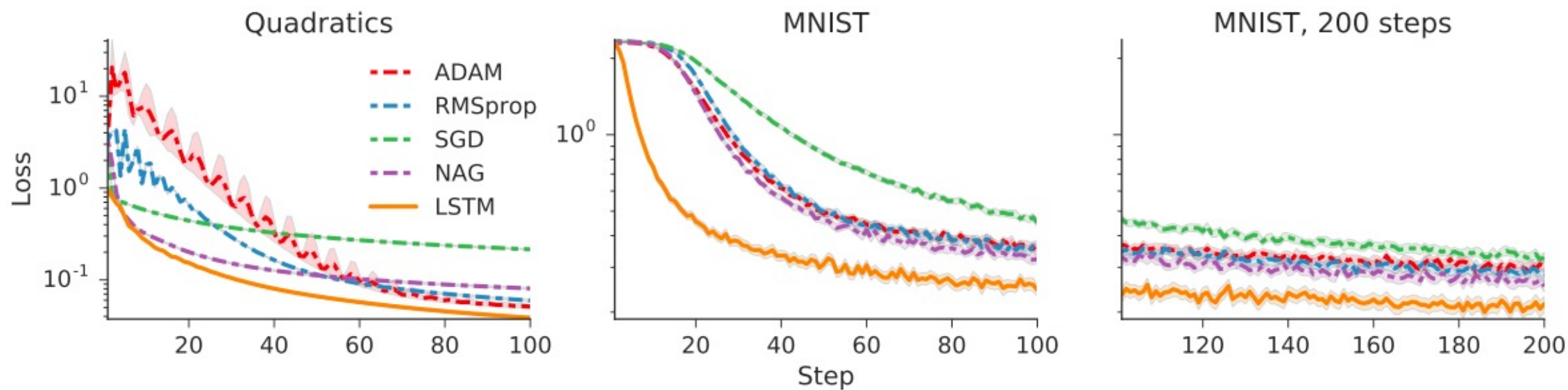
$$\theta_{t+1} \leftarrow \theta_t + g_{\omega}(\nabla_{\theta} L(\theta_t))$$



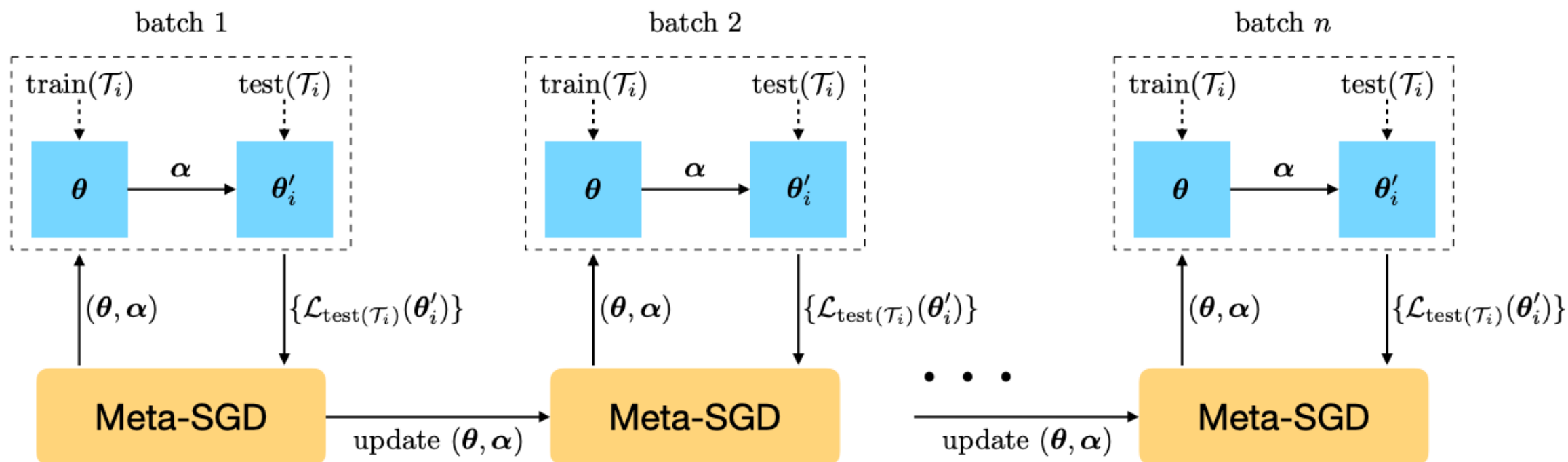
Learning to Optimize



Learning to Optimize



Learning to Optimize



Learn update direction and learning rate separately



Learning to Initialize

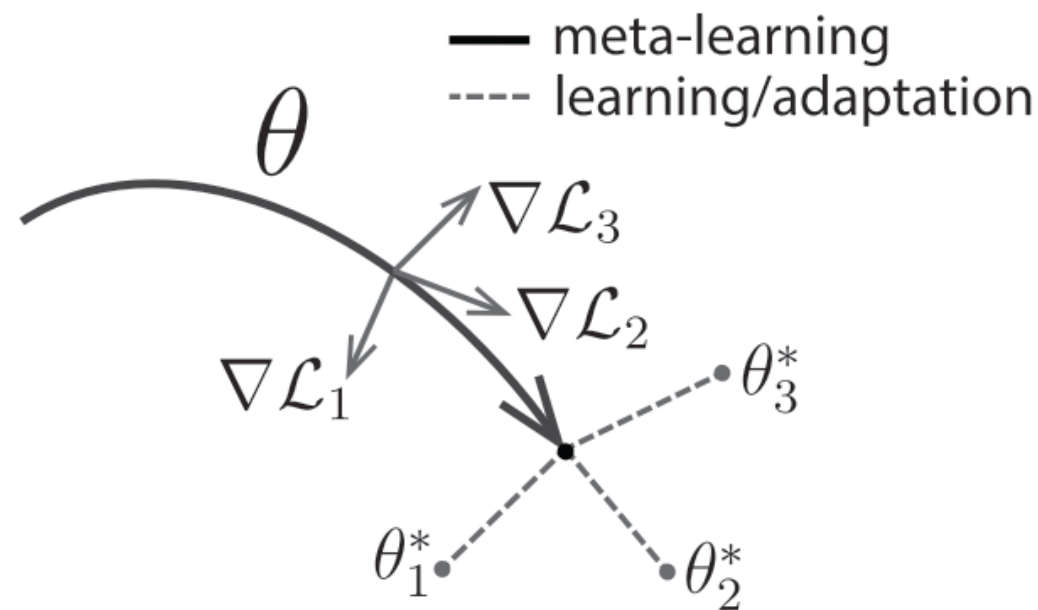
Model-agnostic meta-learning for fast adaptation of deep networks

[C Finn, P Abbeel, S Levine](#) - ... on machine learning, 2017 - proceedings.mlr.press

... for **meta-learning** that is **model-agnostic**, in the sense that it is compatible with any **model** trained with gradient descent and applicable to a variety of different **learning** problems, ...

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- In Model-Agnostic Meta-Learning (MAML), ω is the initialized model parameter θ .
- The goal is to find a good θ , such that only a few steps optimization can obtain good model for a task.



MAML

- The optimization of MAML follows:

$$\theta'_i \leftarrow \theta - \beta \nabla_{\theta} L\left(\theta, D_{train}^{support(i)}\right)$$
$$\theta \leftarrow \theta - \alpha \nabla_{\theta} \sum_{i=1}^M L\left(\theta'_i, D_{train}^{query(i)}\right)$$

- ω is the model parameter θ itself.
- The loss function is same: $L = L^{meta} = L^{task}$.
- It is call model-agnostic because there is no specified meta-learning model for ω .
- Any model can apply MAML.



Algorithm 1 Model-Agnostic Meta-Learning

Require: $p(\mathcal{T})$: distribution over tasks

Require: α, β : step size hyperparameters

1: randomly initialize θ

2: **while** not done **do** Outer loop

3: Sample batch of tasks $\mathcal{T}_i \sim p(\mathcal{T})$

4: **for all** \mathcal{T}_i **do** Inner loop

5: Evaluate $\nabla_{\theta} \mathcal{L}_{\mathcal{T}_i}(f_{\theta})$ with respect to K examples

6: Compute adapted parameters with gradient descent: $\theta'_i = \theta - \alpha \nabla_{\theta} \mathcal{L}_{\mathcal{T}_i}(f_{\theta})$

7: **end for**

8: Update $\theta \leftarrow \theta - \beta \nabla_{\theta} \sum_{\mathcal{T}_i \sim p(\mathcal{T})} \mathcal{L}_{\mathcal{T}_i}(f_{\theta'_i})$

9: **end while**

Inner loop updates model parameter for each task i .

Outer loop updates θ by evaluating each θ'_i on query set.

θ'_i is obtained from θ . Therefore evaluating θ'_i implicitly evaluates θ .



MAML vs. Pre-Trained Model

MAML vs. pre-trained model

- MAML looks for a good initialization to generalize new task.
- Pre-trained model transfers knowledge from a well-learned model on source tasks to a target task by finetuning.

What is the difference here?



MAML vs. Pre-Trained Model

- MAML doesn't require the initialized model θ perform well on each task, but the one-step optimized θ_i' :

$$L(\theta) = \sum_{i=1}^M L\left(\theta_i', D_{train}^{query(i)}\right)$$

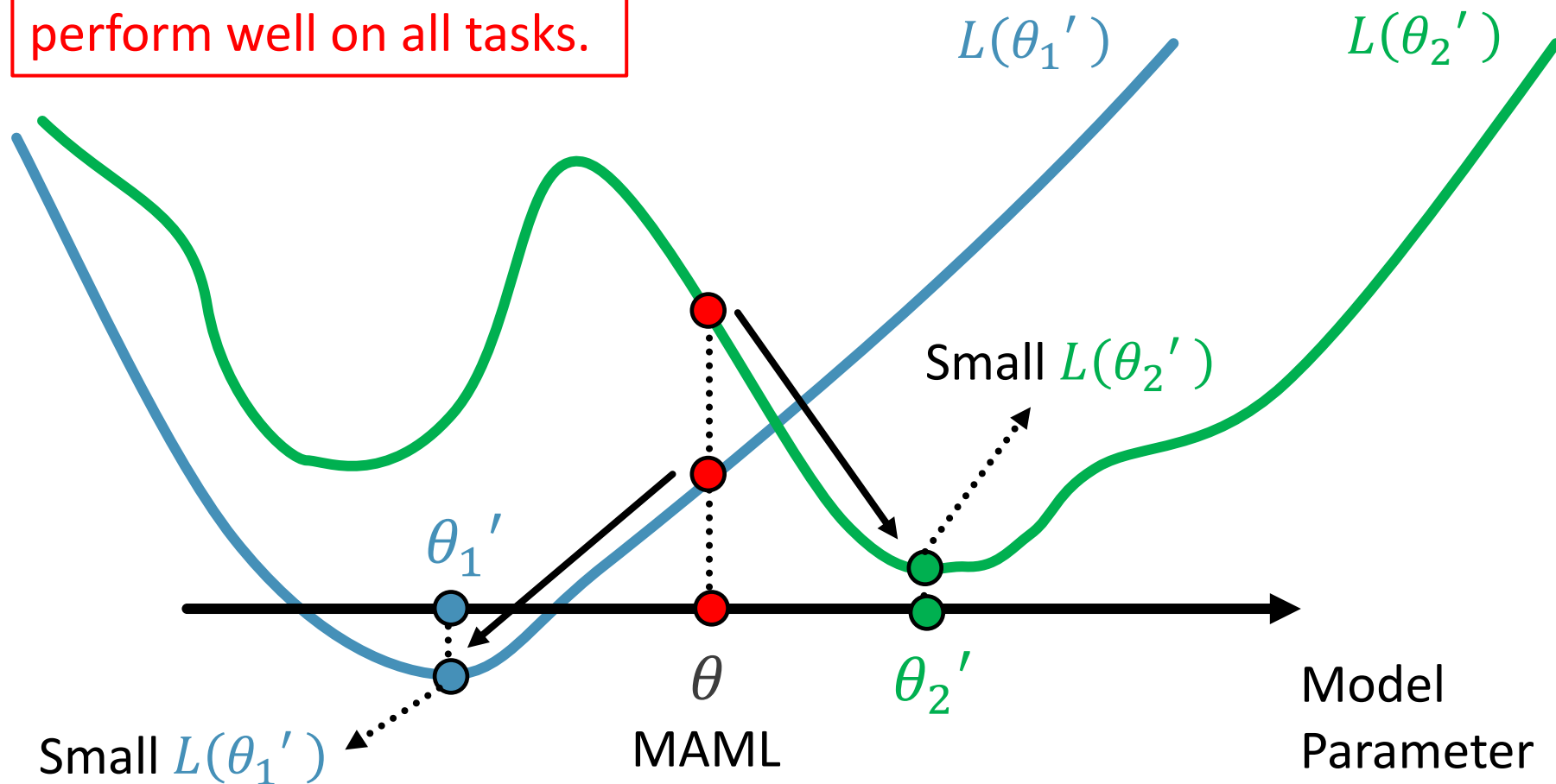
- Pre-trained model usually require the initialized model θ perform well on each task:

$$L(\theta) = \sum_{i=1}^M L\left(\theta, D_{train}^{(i)}\right)$$



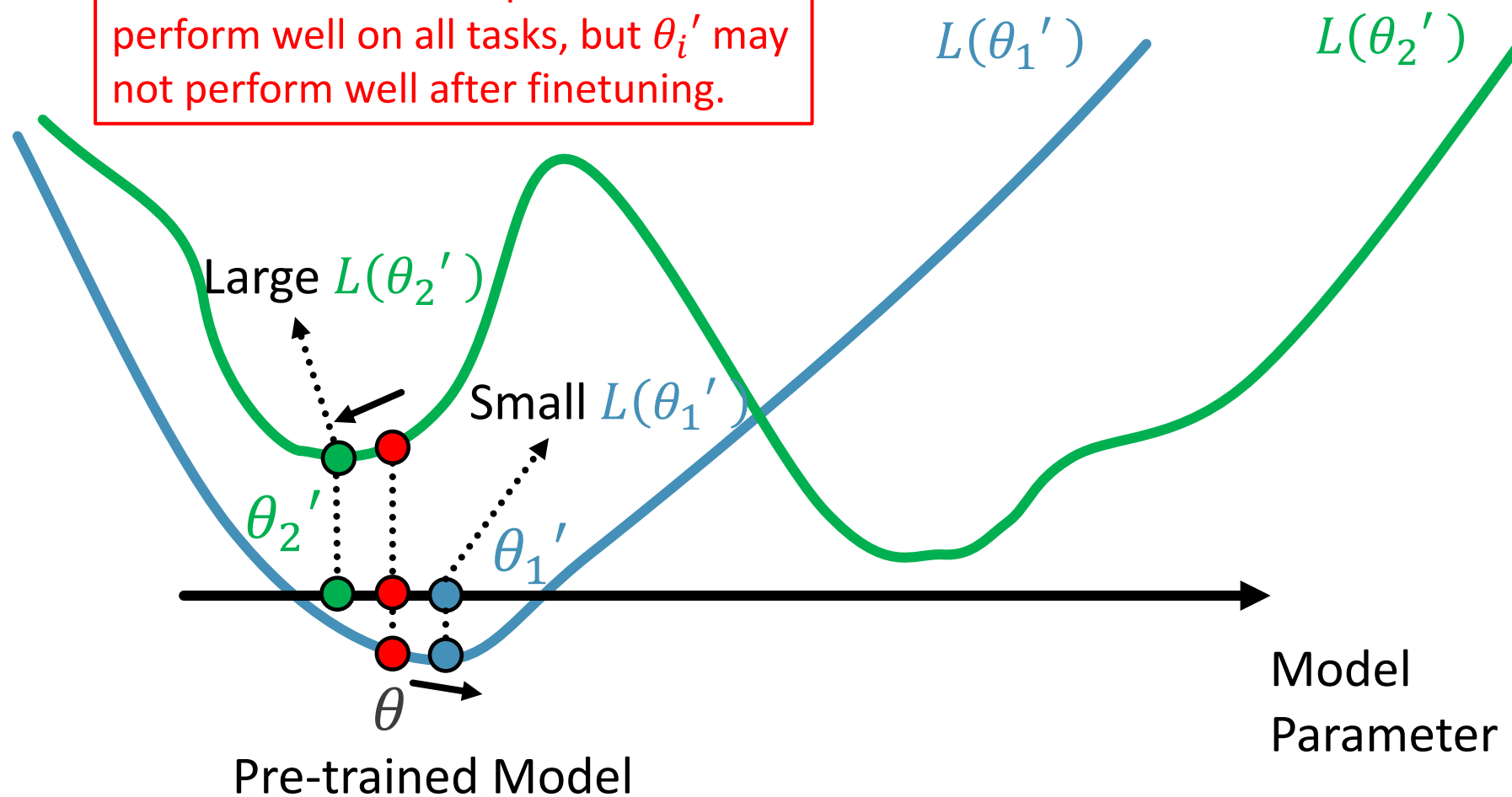
MAML vs. Pre-Trained Model

MAML doesn't require θ perform well on all tasks.



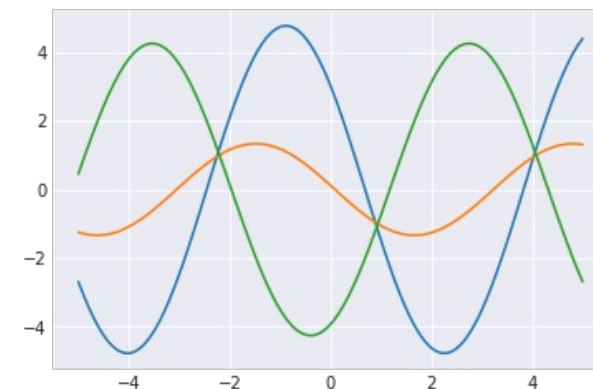
MAML vs. Pre-Trained Model

Pre-trained model requires θ perform well on all tasks, but θ_i' may not perform well after finetuning.

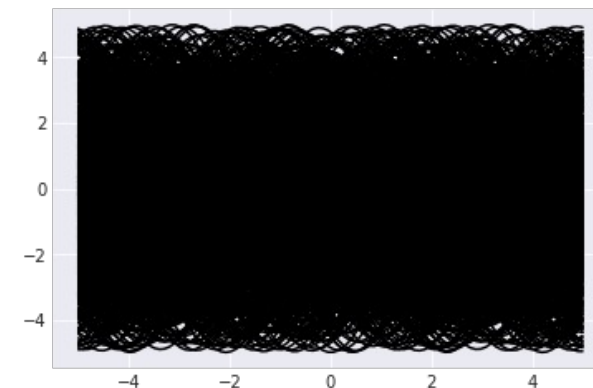


MAML vs. Pre-Trained Model

- Toy example: try to learn sine function $y = a\sin(x + b)$.
- Each combination of a and b is a task.
- The goal is to fit a new sin function based on only a few points.



3 random tasks



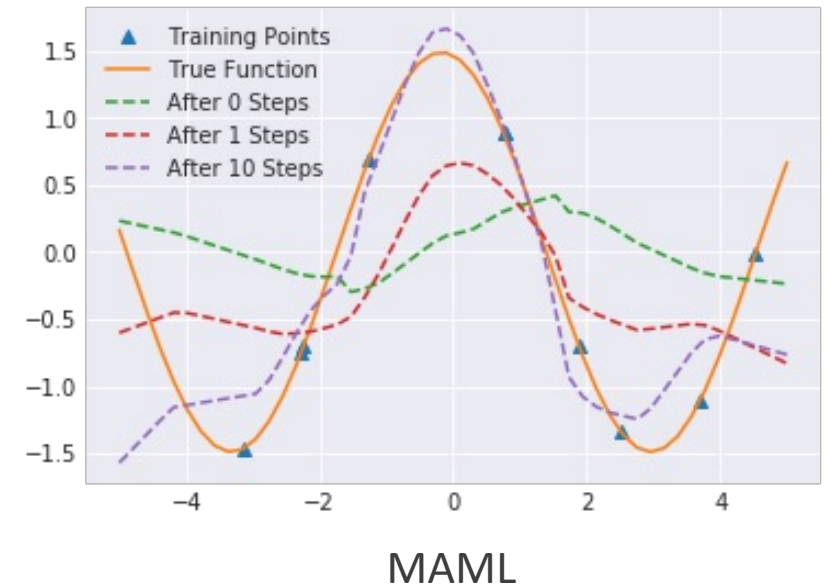
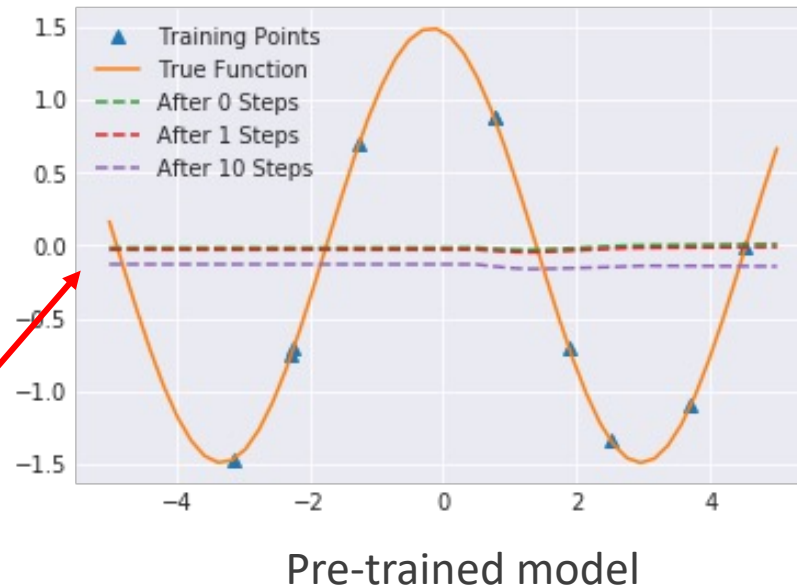
1000 random tasks



MAML vs. Pre-Trained Model

- MAML is able to quickly adapt with only a few datapoints.
- MAML trained model f_θ has learned to model the periodic nature of the sine wave!

Pre-trained model learns a straight line because it has to minimize the error for all tasks.



First-Order MAML

- MAML takes partial derivatives on θ at both inner and outer loop.
- Therefore, the outer loop actually calculates the second-order derivatives, i.e. Hessian.

$$\begin{aligned}
 & \nabla_{\theta} \sum_{i=1}^M L(\theta'_i) \\
 &= \sum_{i=1}^M \nabla_{\theta} L(\theta'_i) \\
 &= \sum_{i=1}^M \begin{bmatrix} \partial L(\theta'_i) / \partial \theta_1 \\ \partial L(\theta'_i) / \partial \theta_2 \\ \vdots \\ \boxed{\partial L(\theta'_i) / \partial \theta_j} \\ \vdots \end{bmatrix}
 \end{aligned}$$

$\theta'_k = \theta - \beta \nabla_{\theta} L(\theta)$

$$\begin{aligned}
 & \partial L(\theta'_i) / \partial \theta_j \\
 &= \sum_k \frac{\partial L(\theta'_i)}{\partial \theta'_k} \boxed{\frac{\partial \theta'_k}{\partial \theta_j}}
 \end{aligned}$$

$$\frac{\partial \theta'_k}{\partial \theta_j} = \begin{cases} 1 - \beta \frac{\partial L(\theta)}{\partial \theta_k \partial \theta_j}, & k = j \\ -\beta \frac{\partial L(\theta)}{\partial \theta_k \partial \theta_j}, & k \neq j \end{cases}$$

First-Order MAML

- The second order derivative $\frac{\partial L(\theta)}{\partial \theta_k \partial \theta_j}$ is the element of Hessian matrix $H_\theta(L)$.

- We can rewrite the outer loop gradient as:

$$\nabla_\theta L(\theta_i') = (I - \beta H_\theta(L)) \nabla_{\theta_i'} L(\theta_i')$$

- First-Order MAML (FOMAML) calculates the approximation by simply setting the Hessian matrix at 0:

$$\nabla_\theta L(\theta_i') \approx \nabla_{\theta_i'} L(\theta_i')$$



First-Order MAML

8: Update $\theta \leftarrow \theta - \beta \nabla_{\theta} \sum_{\tau_i \sim p(\tau)} \mathcal{L}_{\tau_i}(f_{\theta'_i})$
9: **end while**

Replacing θ by θ'_i highly improves the efficiency without loss of much accuracy.

| MiniImagenet (Ravi & Larochelle, 2017) | 5-way Accuracy | |
|---|-------------------------------------|-------------------------------------|
| | 1-shot | 5-shot |
| fine-tuning baseline | 28.86 \pm 0.54% | 49.79 \pm 0.79% |
| nearest neighbor baseline | 41.08 \pm 0.70% | 51.04 \pm 0.65% |
| matching nets (Vinyals et al., 2016) | 43.56 \pm 0.84% | 55.31 \pm 0.73% |
| meta-learner LSTM (Ravi & Larochelle, 2017) | 43.44 \pm 0.77% | 60.60 \pm 0.71% |
| MAML, first order approx. (ours) | 48.07 \pm 1.75% | 63.15 \pm 0.91% |
| MAML (ours) | 48.70 \pm 1.84% | 63.11 \pm 0.92% |



Reptile

- Reptile further simplify FOMAML.

k time update instead of 1

Algorithm 1 Reptile (serial version)

Initialize ϕ , the vector of initial parameters

for iteration = 1, 2, ... **do**

 Sample task τ , corresponding to loss L_τ on weight vectors $\tilde{\phi}$

 Compute $\tilde{\phi} = U_\tau^k(\phi)$, denoting k steps of SGD or Adam

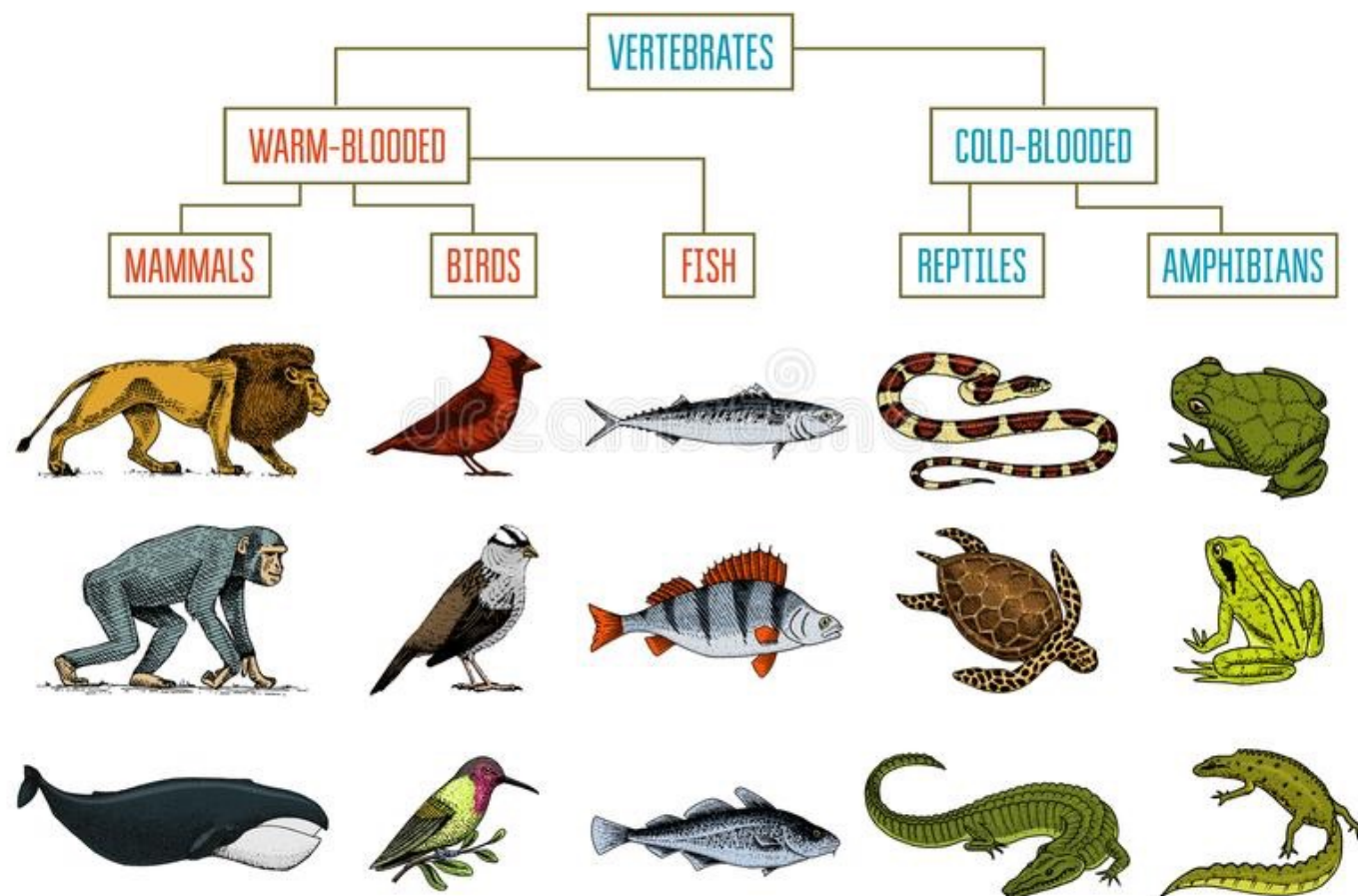
 Update $\phi \leftarrow \phi + \epsilon(\tilde{\phi} - \phi)$

end for

Simply use the direction instead of calculating gradient



CLASSIFICATION OF ANIMALS



Learning to Weight

- During optimization, we may assign different weights to different training samples, according to its learning difficulty.

$$\theta \leftarrow \theta - \alpha \nabla_{\theta} \sum_{i=1}^N w(\mathbf{x}_i) l(\theta, \mathbf{x}_i)$$

- In this manner, difficult (frequently misclassified) samples are assigned higher weights.
- For example, Focal loss assigns weight by:

$$w(\mathbf{x}_i) = (1 - p_{y_i})^{\gamma}$$

Hand-crafted
design!

where p_{y_i} is the probability belonging to its ground truth y_i .



Learning to Weight

- Can we learn a mapping function from the sample \mathbf{x}_i to its weight $w(\mathbf{x}_i)$?
- Of course! Simply train an MLP to learn the relationship:

$$\theta \leftarrow \theta - \alpha \nabla_{\theta} \sum_{i=1}^N F_{\omega}(l(\theta, \mathbf{x}_i)) l(\theta, \mathbf{x}_i)$$

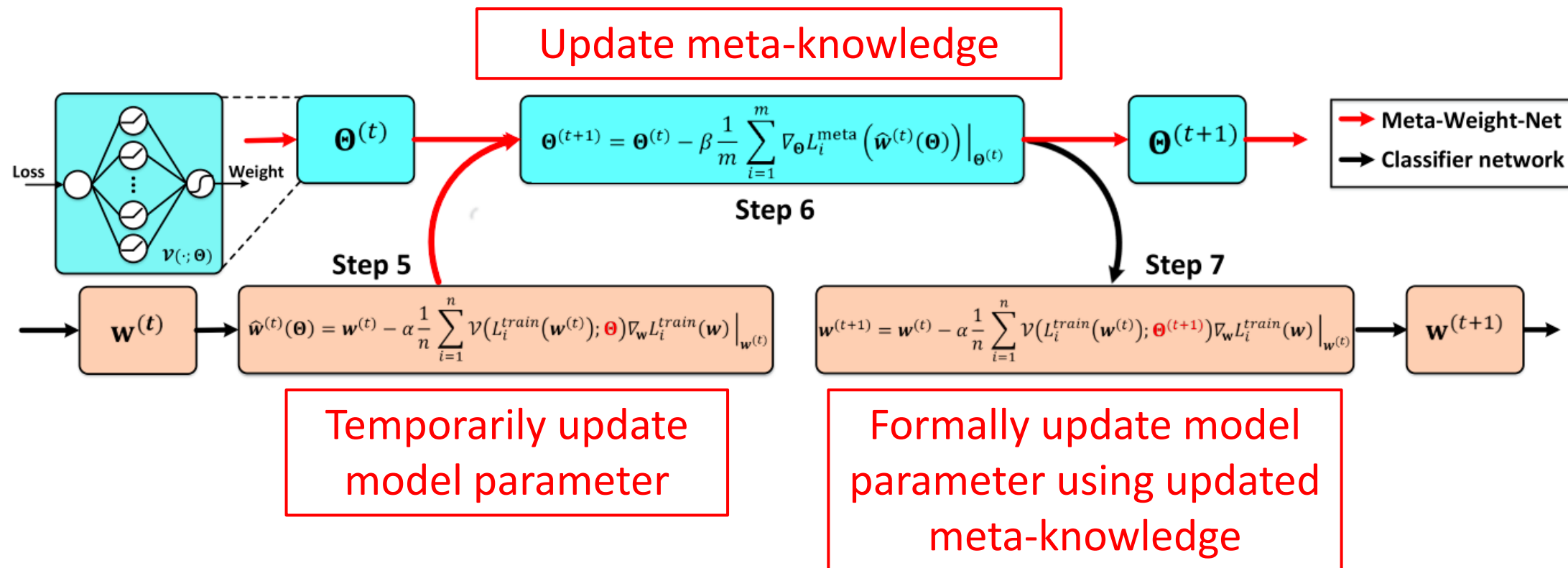
where $F_{\omega}(l(\theta, \mathbf{x}_i))$ takes the training loss as input and output the corresponding weight.



Learning to Weight

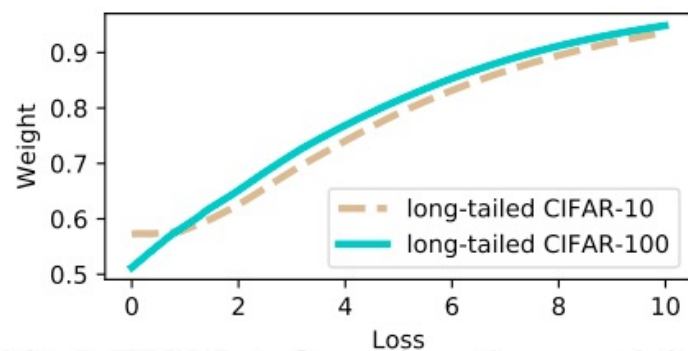
Meta-weight-net: Learning an explicit mapping for sample weighting
 J. Shu, Q. Xie, L. Yi, Q. Zhao, S. Zhou... - Advances in neural ..., 2019 - proceedings.neurips.cc
 ... In contrast, with the explicit yet simple **Meta-Weight-Net**, our method can learn the weight
 in a more stable way, as shown in Fig. 6, and can be easily generalized from a certain task to ...
 ☆ Save 📄 Cite Cited by 683 Related articles All 10 versions 🔗

- Again, we use $D_{train}^{support}$ to optimize θ , and use D_{train}^{query} to optimize ω .

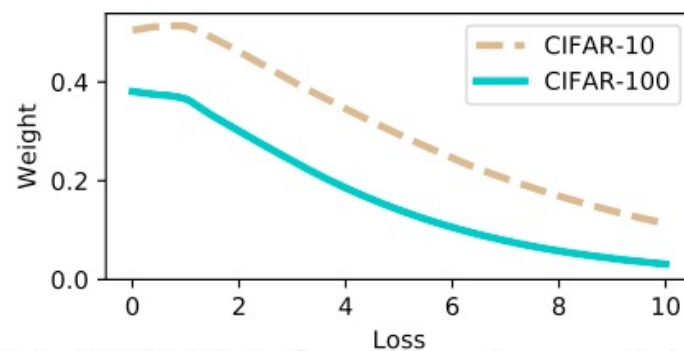


Learning to Weight

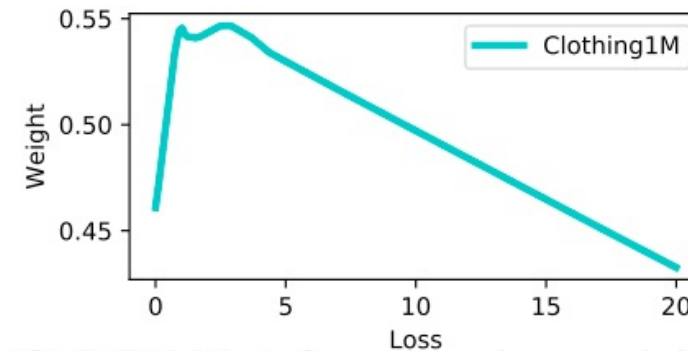
- The weighting function is learned based on the distribution of the dataset.



(d) MW-Net function learned in class imbalance case



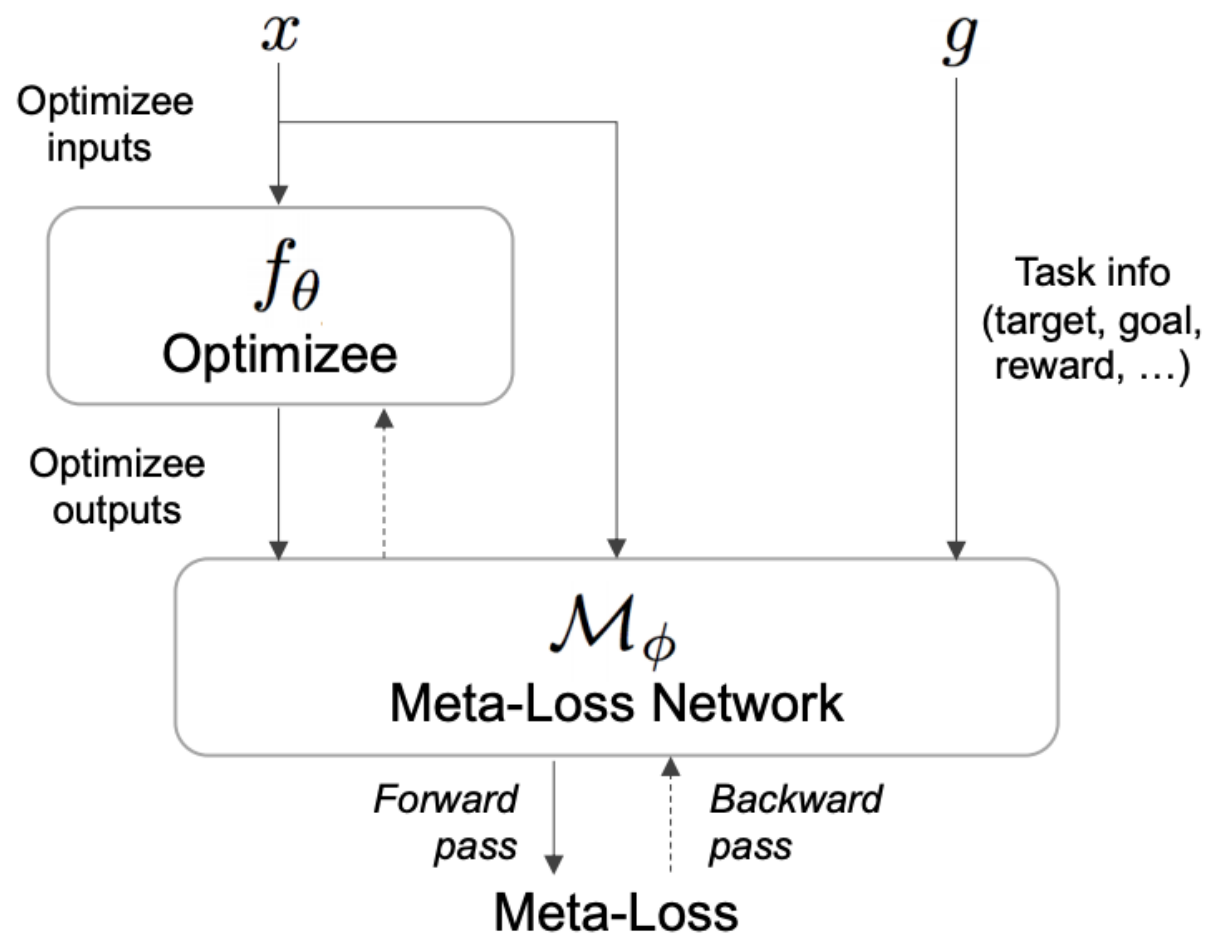
(e) MW-Net function learned in corrupter labels case



(f) MW-Net function learned in real Clothing1M dataset



Learning to Reward

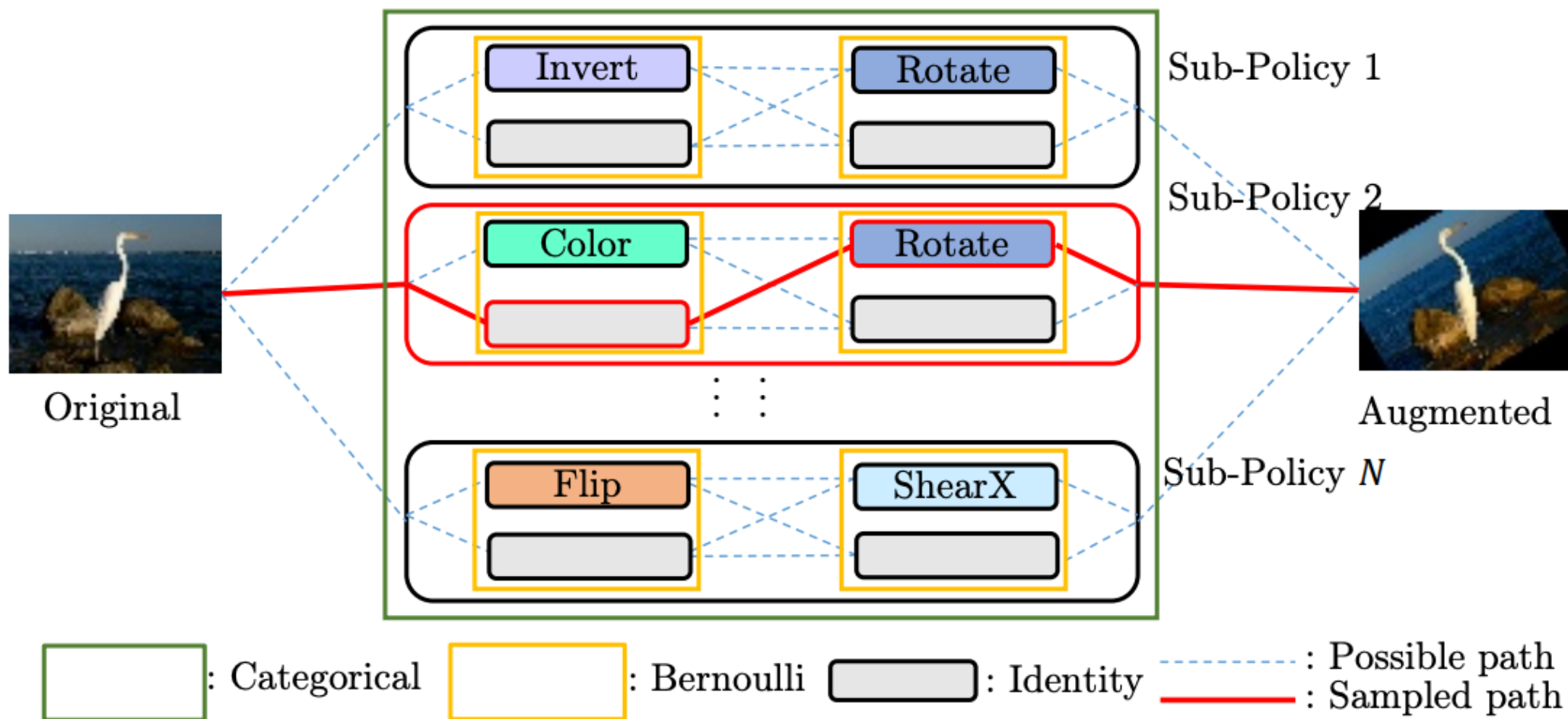


Learning to Augment

- The data augmentation operation is wrapped up in inner optimization, which is conventionally hand-designed.
 - E.g. crop, zoom, flip, rotate, etc.
- When ω defines the data augmentation strategy, it can be learned by the outer optimization, in order to maximize validation performance.



Learning to Augment

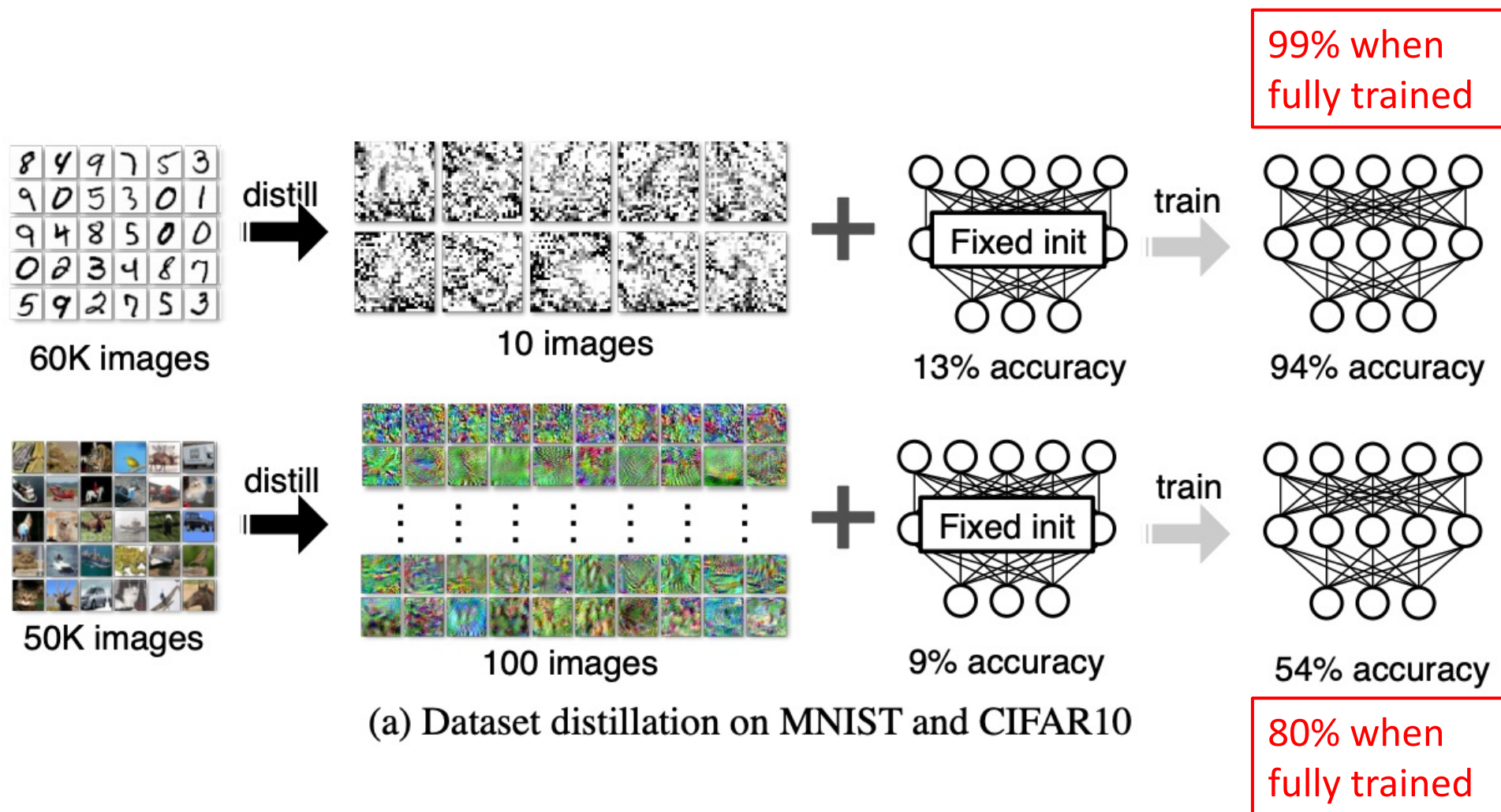


Dataset Distillation

- In bi-level optimization, we always use the same support data to optimize model parameter θ .
- Can the support data itself be the meta-knowledge ω ?
 - Select the most significant samples to train the model.
 - Only a few selected samples can achieve high performance.

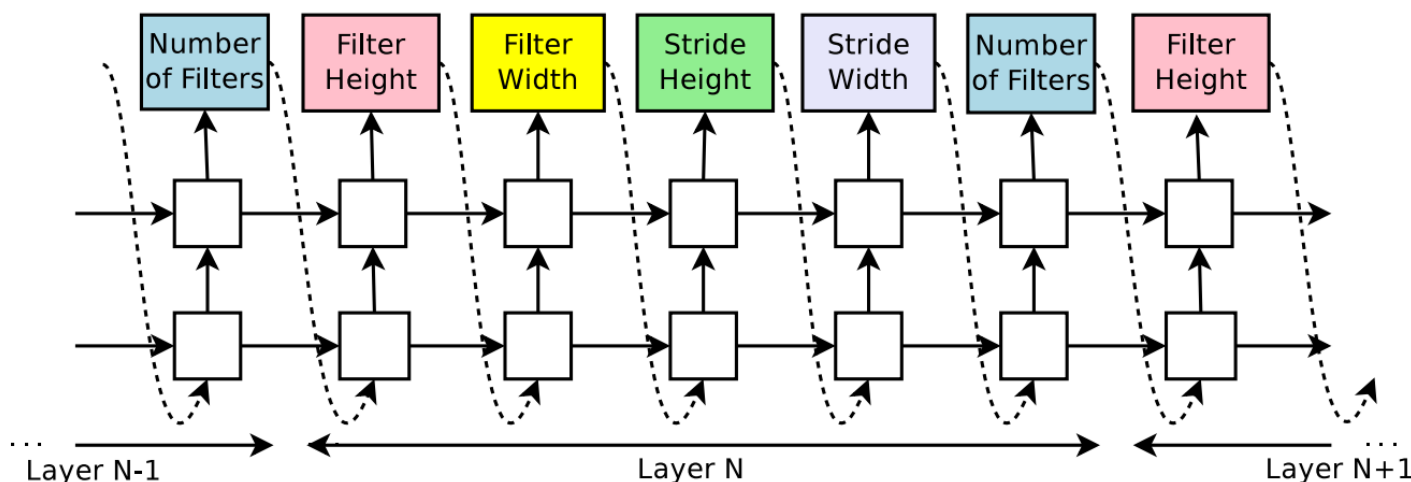


Dataset Distillation



Neural Architecture Search

- ω specifies the architecture of a neural network.
 - E.g. number of filters, filter size, stride and pooling size, activation functions, shortcut connections, etc.
- The search space is usually hard to define, and optimize.
 - Most search spaces are broad, and the space of architectures is **not trivially differentiable**.



Reinforcement learning
is usually adopted to
search the spaces.





MODEL-BASED METHOD



Model-Based Method

- The optimization of model network f_{θ} in all optimization-based methods are still based on gradient descend.
- In the inner loop, given ω , we optimize θ .

$$\theta^*(\omega) = \underset{\theta}{\operatorname{argmin}} L^{\text{task}}(\theta, \omega, D_{\text{train}}^{\text{support}})$$

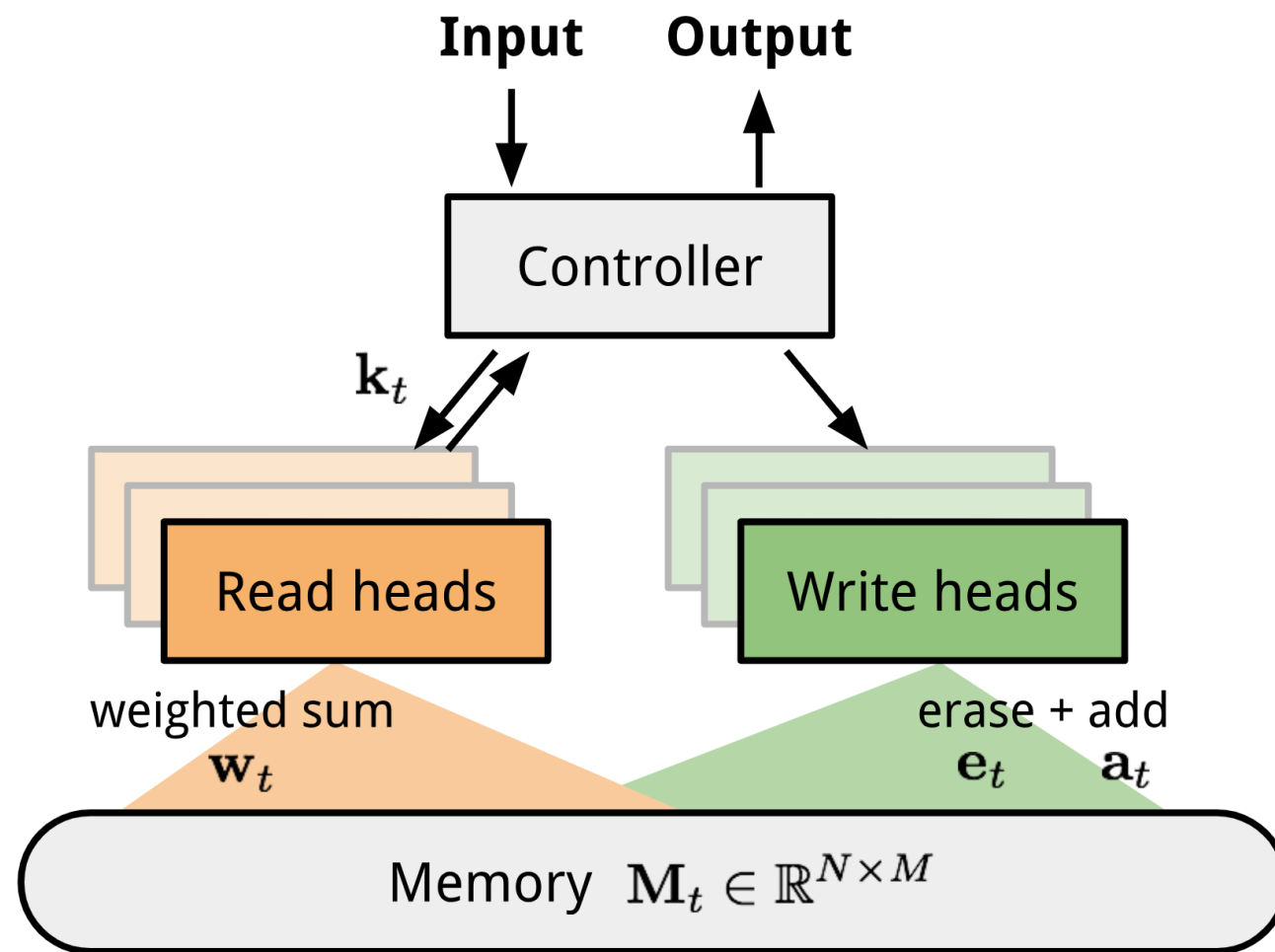
- Can we omit this optimization step and directly obtain θ^* ?

$$\theta^*(\omega) = g_{\omega}(D_{\text{train}}^{\text{support}})$$

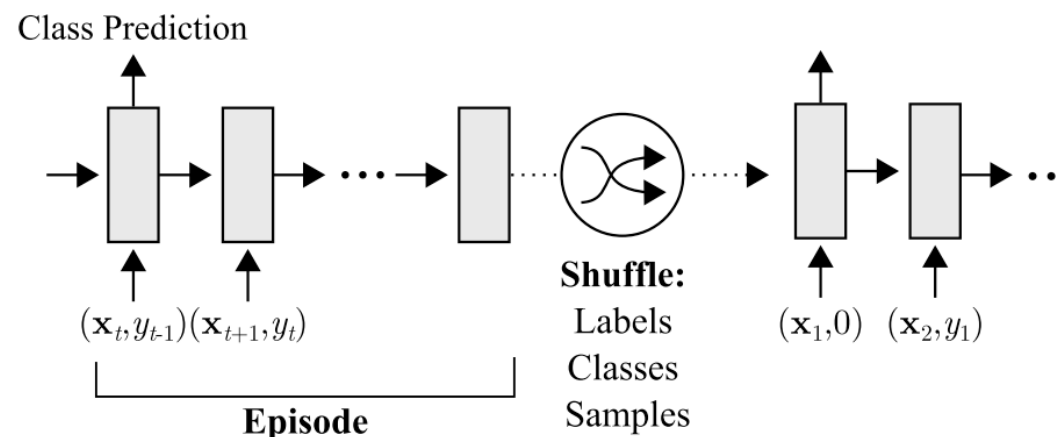
Model-based methods adopt the meta-knowledge ω to directly generate a model.



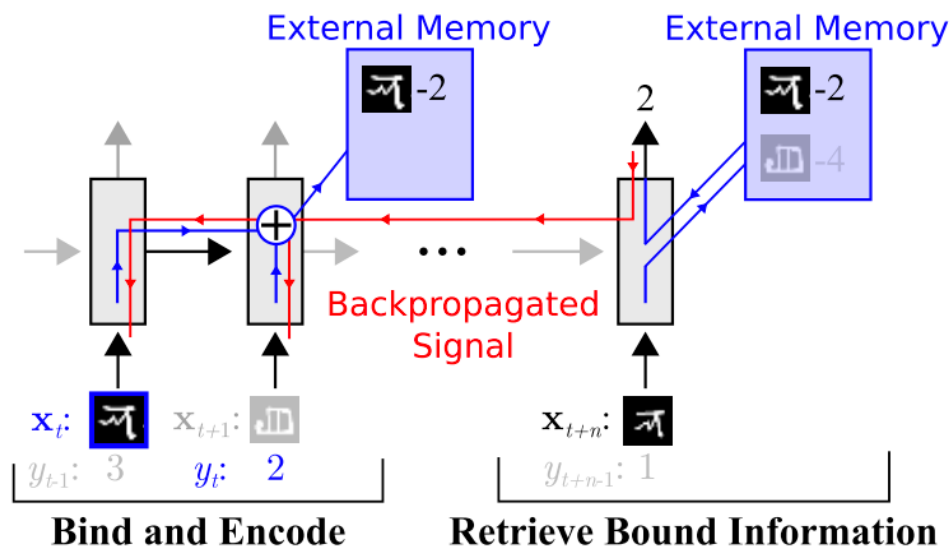
Memory-Augmented Neural Networks



Memory-Augmented Neural Networks



Meta-knowledge ω learns proper representation to read and write with memory.

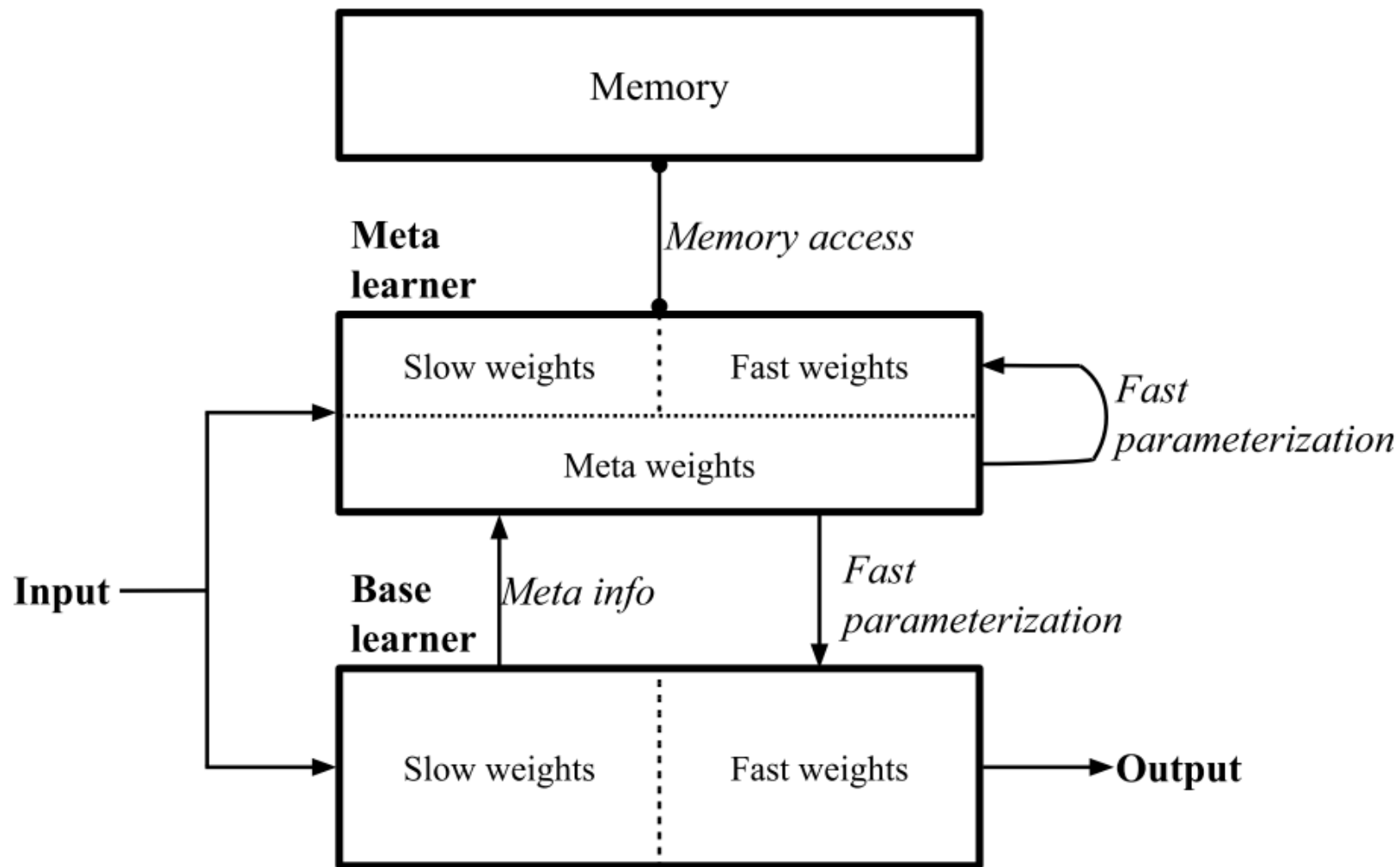


Meta Networks

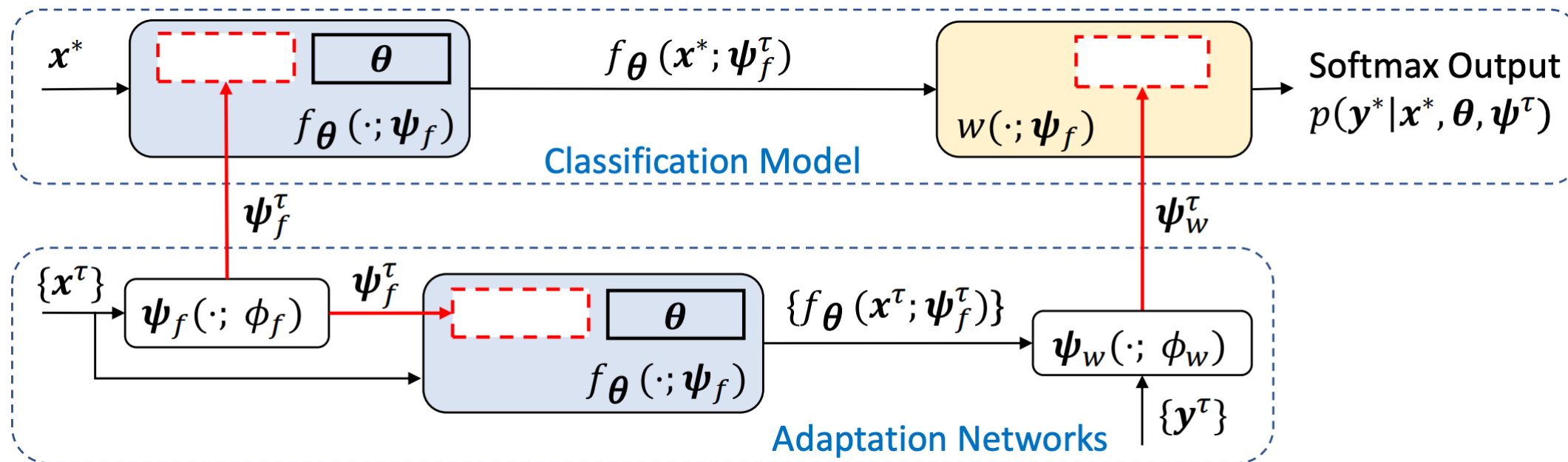
- **Slow weights**: weights that are learned from an optimization process like SGD.
- **Fast weights**: weights that are directly generated by another network.
- In MetaNet, loss gradients are used as meta information to populate models that learn fast weights.
 - Slow and fast weights are combined to make predictions in neural networks.



Meta Networks



CNAPs



The model is not generated from scratch. We generate the adaptation model to new tasks, instead of optimize the model to new tasks.





METRIC-BASED METHOD



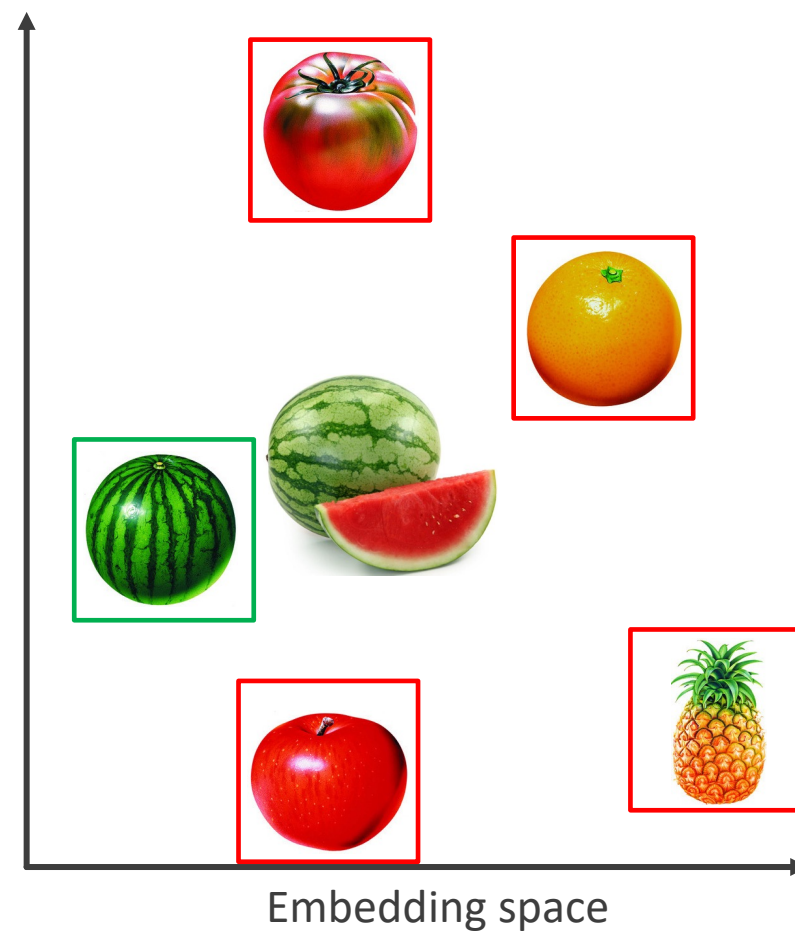
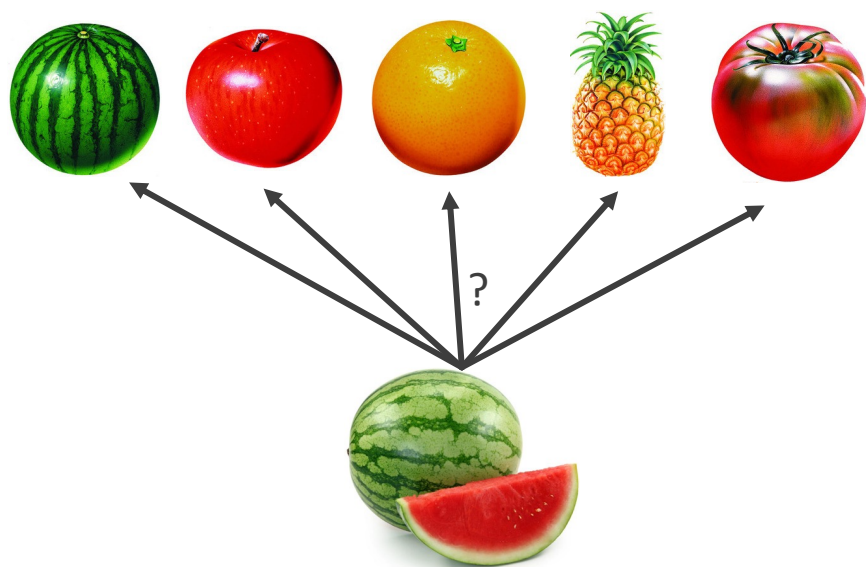
Metric-Based Method

- Previously, we always have a model f_θ to output class score $f_\theta(\mathbf{x})$, no matter f_θ is optimized by gradient descend with meta knowledge or directly generated by meta model.
- Do we have to use a model to do prediction? Is there any machine learning method that doesn't have a model?

k NN



Metric-Based Method



Metric-Based Method

- Metric-based methods learn an embedding network F_{ω} .
- The learned representation is suitable for recognition by simple similarity comparison between query and support instances.
- Take one-shot learning as an example, at testing phase, we simply calculating the similarity between:

$$F_{\omega}(\mathbf{x}_{test}^{query}) \quad \text{and} \quad F_{\omega}(\mathbf{x}_{test}^{support(j)})$$

- It can also be treated as model-based method with only one linear layer.

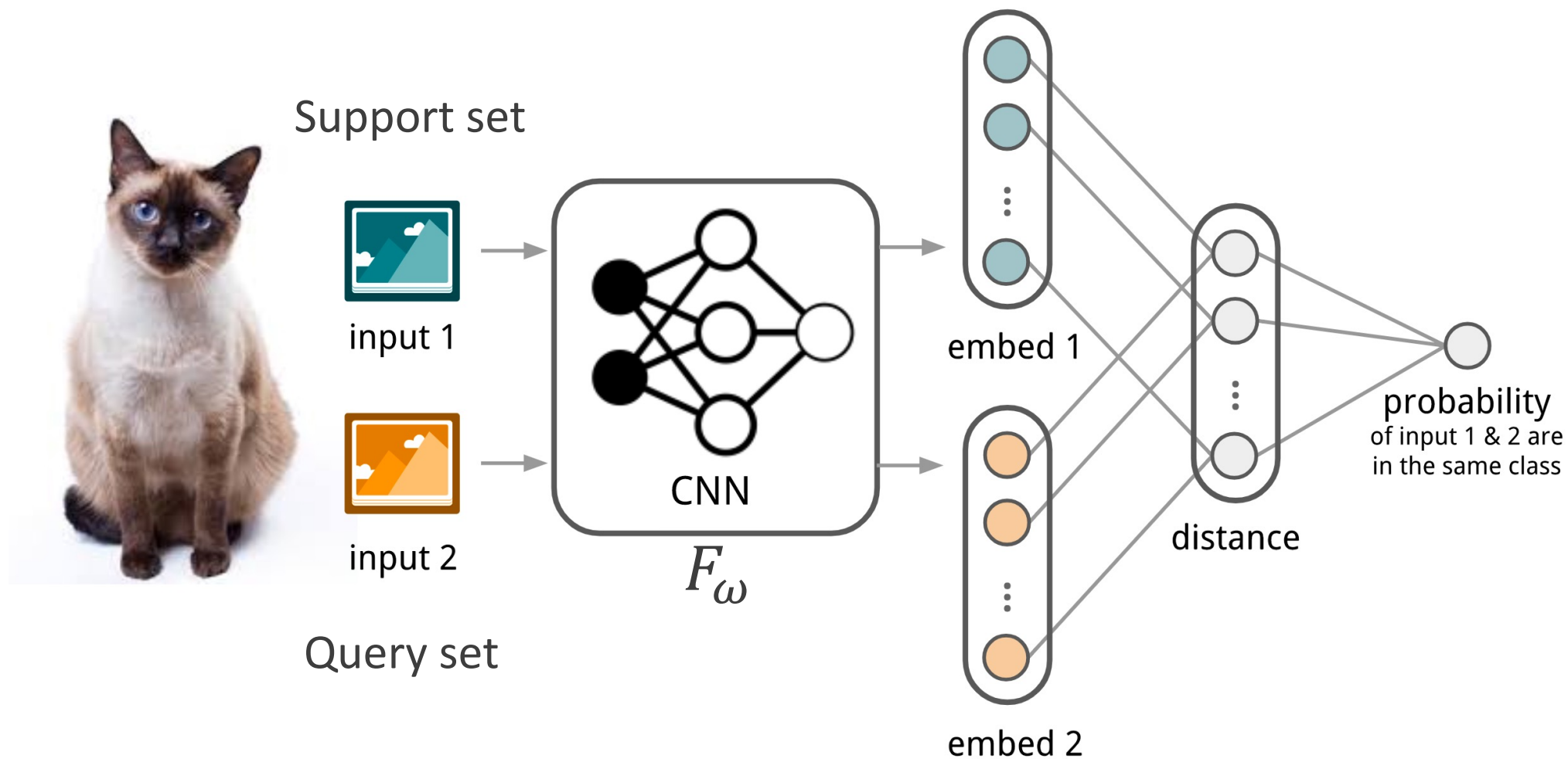


Metric-Based Method

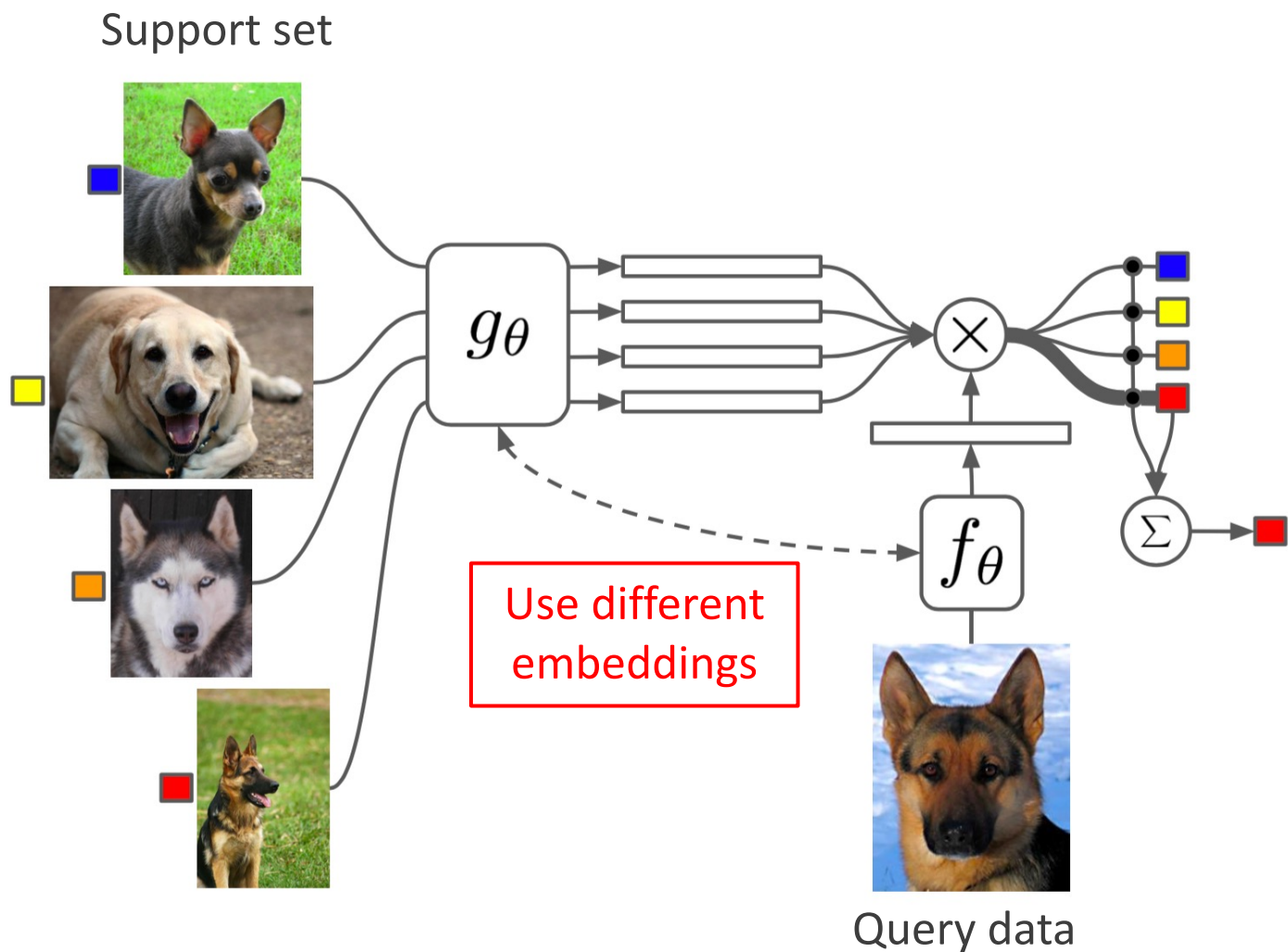
- Siamese networks
- Matching networks
- Prototypical networks
- Relation networks
- Graph networks



Siamese Networks



Matching Networks



Matching Networks

- Simple version:

$$a(\hat{\mathbf{x}}, \mathbf{x}_i) = \exp\left(\cos(F_\omega(\hat{\mathbf{x}}), G_\omega(\mathbf{x}_i))\right) / \sum_{j=1}^k \exp\left(\cos(F_\omega(\hat{\mathbf{x}}), G_\omega(\mathbf{x}_j))\right)$$

- Full context version:

$$\hat{\mathbf{h}}_k, \mathbf{c}_k = \text{LSTM}(F(\hat{\mathbf{x}}), [\mathbf{h}_{k-1}, \mathbf{r}_{k-1}], \mathbf{c}_{k-1})$$

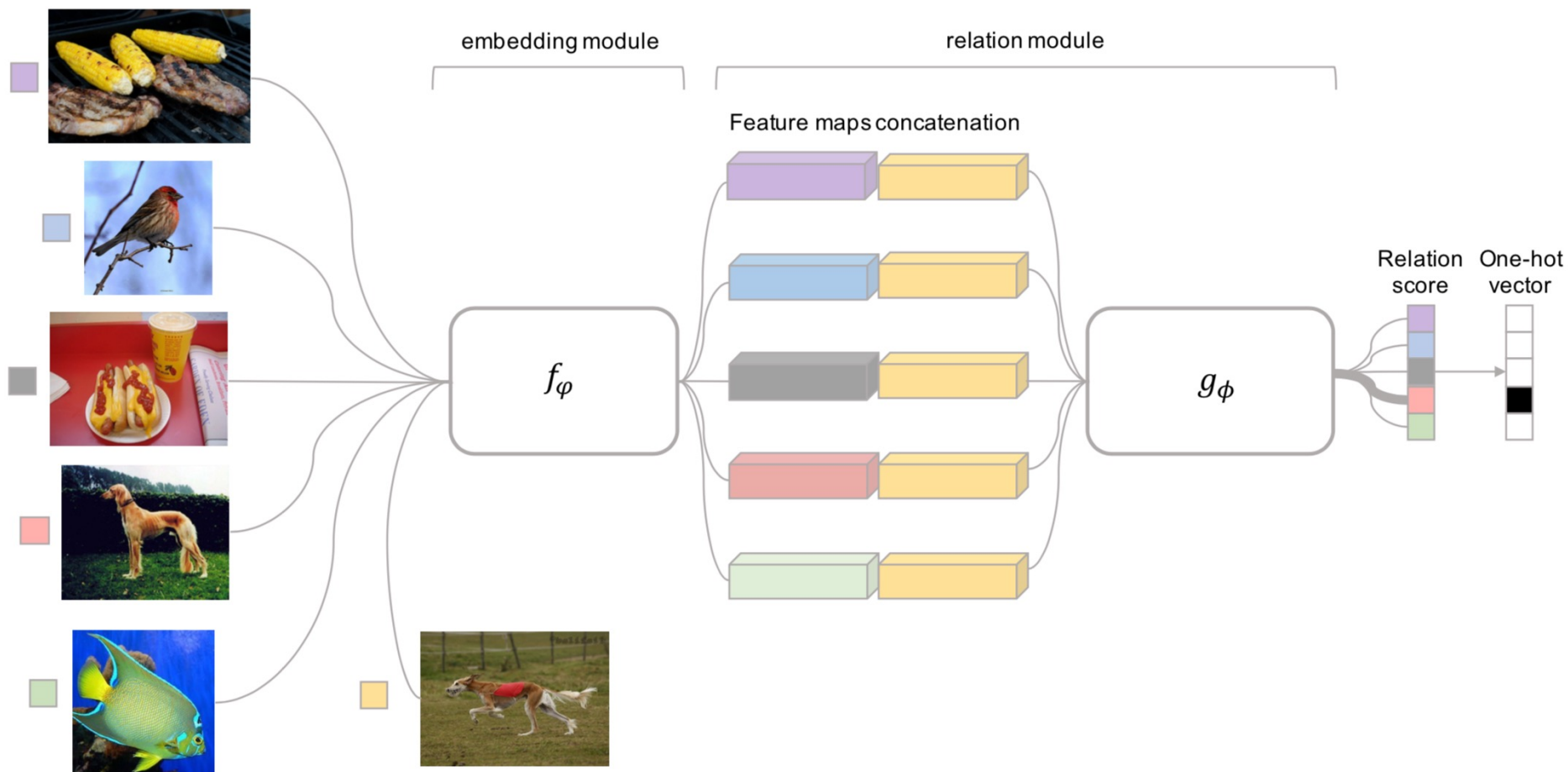
$$\mathbf{h}_k = \hat{\mathbf{h}}_k + F(\hat{\mathbf{x}})$$

$$\mathbf{r}_{k-1} = \sum_{i=1}^{|S|} a(\mathbf{h}_{k-1}, G(\mathbf{x}_i)) G(\mathbf{x}_i)$$

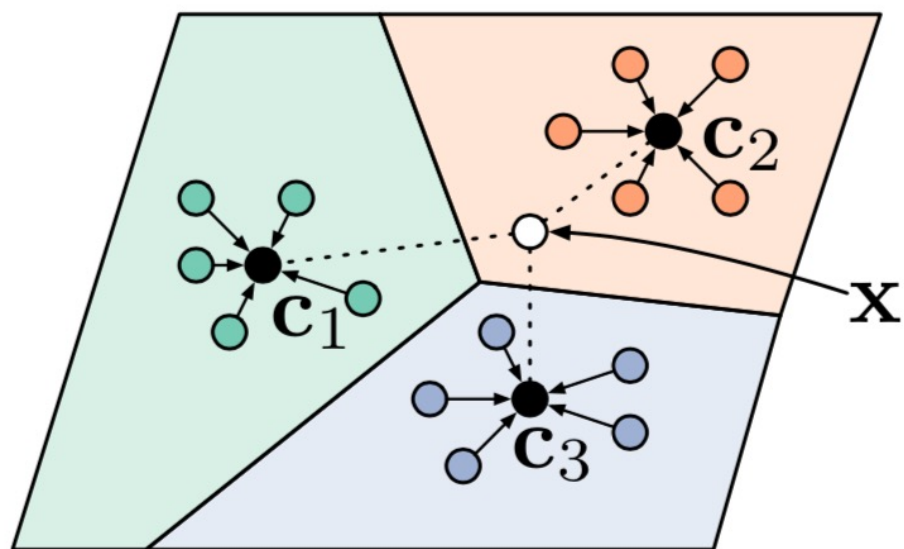
$$a(\mathbf{h}_{k-1}, G(\mathbf{x}_i)) = \exp\left(\mathbf{h}_{k-1}^T G(\mathbf{x}_i)\right) / \sum_{j=1}^{|S|} \exp\left(\mathbf{h}_{k-1}^T G(\mathbf{x}_j)\right)$$



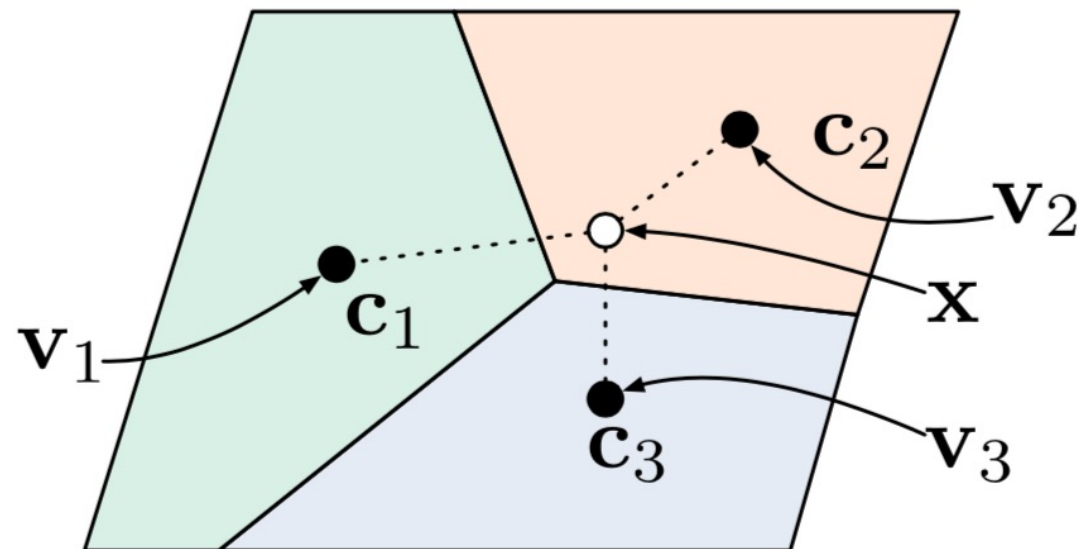
Relation Networks



Prototypical Networks



(a) Few-shot



(b) Zero-shot



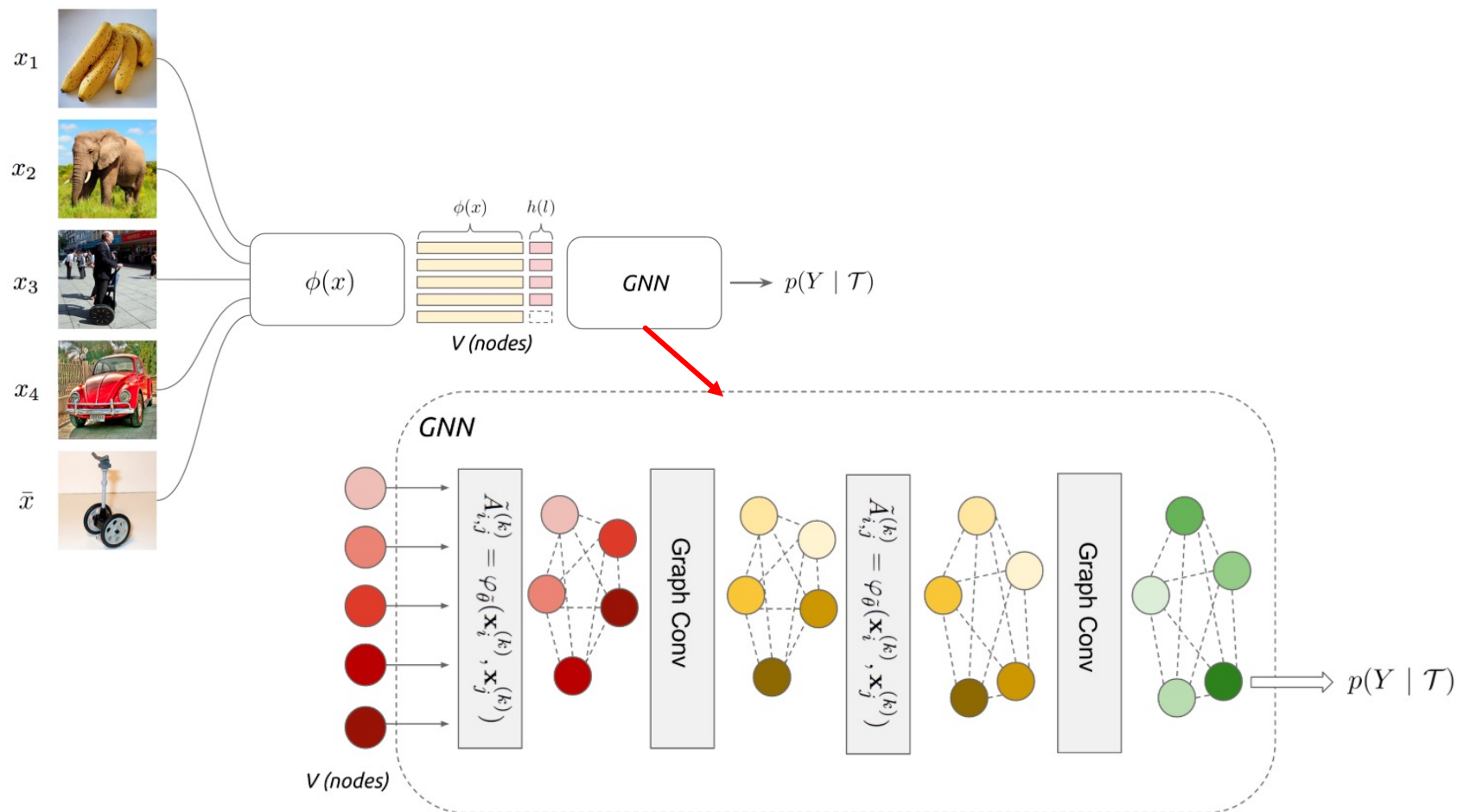
Zero-Shot Learning

- One-shot is difficult enough. How can zero-shot work?
- Zero-shot learning differs from few-shot learning in that instead of being given a support set of training points, we are given a class meta-data vector \mathbf{v}_k for each class.
 - For example, \mathbf{v}_k can be a sentence embedding for text description of the image.
 - The “zero” in zero-shot is for the labelled support set, but we can utilize other information instead.
- We can simply build a mapping between meta-data vector \mathbf{v}_k to its prototype:

$$\mathbf{c}_k = g_{\omega}(\mathbf{v}_k).$$



Graph Networks



Metric-Based Method

Generally, two steps:

- Build an embedding network F_ω .
- Model the relation between $F_\omega(\hat{x})$ and $F_\omega(x_i)$, and output the probabilities.



Conclusion

After this lecture, you should know:

- What is meta-learning and learning to learn.
- How can we utilize meta-knowledge.
- What is few-shot learning and N -way- k -shot.
- What is the difference between optimization-based, model-based and metric-based meta-learning.



Reference & Suggested Reading

- Meta Learning: Learn to Learn
- CS 330: Deep Multi-Task and Meta Learning
- Meta-Learning: Learning to Learn Fast
- T. Hospedales, A. Antoniou, P. Micaelli, and A. Storkey, “Meta-Learning in Neural Networks: A Survey,” in *arXiv*, 2020.



Thank you!

- Any question?
- Don't hesitate to send email to me for asking questions and discussion. 😊

